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ECONOMISTS and other analysts seek to measure expectations of future interest rates because such expectations have important effects on economic behavior. Changes in expectations can lead to changes in economic activity, both at the level of the individual firm or consumer, and at the level of the national economy. For example, interest rate expectations enter into investment decisions of firms, portfolio decisions of financial intermediaries and other investors, and borrowing decisions of state and local governments. If these groups alter their expectations of the future level of interest rates, changes in investment, portfolio, and borrowing decisions will occur which affect not only each group individually, but which also affect the level of economic activity in the economy as a whole. Consequently, policymakers and researchers have been interested in measuring market expectations of interest rates — first, to understand the behavior of economic units in individual markets, and second, to monitor changes in expectations which result from policy actions, in order to judge the impact which the policy may have on the economy.

For example, consider the discussion surrounding the recently aborted Federal income tax rebate. The argument for such a policy was that it would stimulate consumer spending, and thus stimulate aggregate output and employment. However, there was considerable concern that the policy would cause an upward revision of short-term interest rate expectations if there were general agreement that the Treasury would have to increase its borrowing substantially during the second half of 1977 to finance the increased deficit. Under such circumstances, much, if not all, of the alleged stimulus that would be provided by the tax rebate could be offset by the negative impact of higher interest rate expectations on firms' decisions to invest in real capital. Such a negative effect arises because the higher the expected level of future interest rates, the less profitable the income stream associated with each particular investment project. The examination of such effects of policy actions would be made much easier if market expectations of future interest rates were readily observable.

A considerable amount of economic research has been devoted to formulating measures of market expectations of interest rates, since data on expectations are not directly observable unless survey methods are used. Efforts at measurement have taken the form of everything from "informed judgement" to elaborate econometric models. Another means of obtaining an estimate of the level of short-term interest rates expected to prevail at some future date has become available since early 1976. This method employs the yield quotations of the futures market in U.S. Treasury bills. These quotations, which are available on a daily basis, embody market expectations of future short-term interest rates. This paper focuses on the information about market expectations which can be obtained from yields on Treasury bill futures contracts.

THE ROLE OF THE TREASURY BILL FUTURES MARKET

The futures market in three-month U.S. Treasury bills was opened on the International Monetary Market of the Chicago Mercantile Exchange in January 1976, soon after the opening of a mortgage futures market on the Chicago Board of Trade in October 1975.¹ Both of these futures markets in financial instruments operate in essentially the same way as the traditional commodity futures markets. Futures trading in financial instruments allows the separation of the risk of unexpected interest rate movements from other types of risk. Futures contracts can be used to hedge against interest rate movements in order to protect actual or expected cash positions of market participants. Profits are thereby protected in much the same way as hedging in commodity futures markets protects against price fluctuations of a particular commodity. Speculation is facilitated by the existence of futures markets, which allow the assumption of risks on a daily basis.

¹For details on the Treasury bill futures market, see the accompanying section: "Characteristics of the Treasury Bill Futures Market."

*The authors gratefully acknowledge the assistance of Ms. Jeanne Rickey and the Statistical Department of the Chicago Mercantile Exchange for providing data used in this paper.
Characteristics of the Treasury Bill Futures Market

The Treasury bill futures market began active trading on January 6, 1976, in contracts of three-month (thirteen-week) U.S. Treasury bills for delivery in March, June, September, and December. Originally, there were only four contracts traded, the latest being for delivery only one year in the future. But in July 1976 the number of contracts was increased to six, the latest being for delivery eighteen months in the future.

The size of each contract is $1 million, in terms of the face value at maturity. Thus, a sale of eight futures contracts of March 1978 Treasury bills is a sale of $8 million of thirteen-week Treasury bills to be delivered in March 1978 at an agreed upon price. Similarly, a purchase of eight futures contracts of March 1978 Treasury bills is a purchase of $8 million of thirteen-week Treasury bills to be delivered in March 1978 at an agreed upon price. If held to delivery, a futures contract is settled on the business day following the last day of trading in the delivery month.1 Futures trading terminates on the second business day following the Treasury auction of three-month bills in the third week of the delivery month. For example, March 1978 Treasury bill futures contracts are delivered in the third week of March, with the delivered Treasury bills maturing at the end of three months (the third week of June 1978).

Although the size of a single contract is $1 million, a person interested in buying or selling a contract can trade in this futures market on margin. The minimum initial margin is $1,500 per contract, and the commission for executing an order is $60 per contract. By offsetting an initial buy or sell order prior to the delivery date, it is possible to trade in Treasury bill futures contracts with far less money than the $1 million face value of each contract.

Prices in the Treasury bill market are quoted on a discount basis, that is, at a price lower than the face value, and prices in the Treasury bill futures market are also quoted on a discount basis. The interest earned on a Treasury bill, if held to maturity, is the difference between the purchase price and the face value (or par price). Prices in the Treasury bill futures market are quoted in terms of the IMM (International Monetary Market) Index, which represents the difference between the Treasury bill yield (discount) on an annual basis and 100 (face value or par).2 For example, Table I shows the futures price and yield quotations for Treasury bills on March 14, 1977, as published by The Wall Street Journal. The March 1977 futures price at the close of trading (the settlement price) was 95.39, so that the interest rate (yield on a discount basis) on the March 1977 contract was 4.61 percent (100 — 95.39).

Interest-rate risk by individuals willing to bear such risk in return for the possibility of making a profit.2 Futures Markets, Information, and Market Expectations

Trading in futures markets provides information to the cash market about the commodity being traded.3 Prices of futures contracts for delivery of a commodity at a future date provide market participants with information as to the expected pattern of future spot prices of this commodity. This is because information relating to the future state of the market for a particular commodity is utilized by market participants when determining the price at which they are willing to buy or sell futures contracts.

If a trader projects that a commodity's price will be different in the future than at the present time, he will buy or sell contracts for delivery of the commodity at some future date as if his projection were correct. Any trader who has better information about future spot prices than other market participants (or feels that he does) can attempt to make profits by trading on this information, with the result that such information is quickly incorporated into the prices of futures contracts. Thus, the interaction of all traders in the futures market provides price quotations which embody the market's expectations of the future spot prices that will prevail on various delivery dates.
In the case of the futures market in Treasury bills, the yields on futures contracts indicate the pattern of interest rates expected by market participants to prevail in certain months in the future, given currently available information. Any expectation of future interest rates, however arrived at, utilizes information about the current and expected values of variables that are thought to influence the behavior of interest rates. Such variables include measures of the current and future state of the economy, the supply and demand for credit, and the course of monetary and fiscal policy. The futures market in Treasury bills serves the role of a processor of this information. As new information about the course of key factors influencing interest rates becomes available, it is rapidly reflected in futures market prices.4

The expected interest rate for any date in the future which is embodied in the yield on current futures contracts is not necessarily the interest rate that will prevail at that future date. Market participants in the futures market do not have a crystal ball that foretells the future perfectly. Their decisions to buy or sell contracts are based on the information available at the present time. As new information becomes available, market participants may very well revise their expectations. The effect of new information — such as a change in the announced monetary targets, new budget projections, revised projections of the strength of economic activity, new pricing policies by OPEC, and so on — is reflected in changes in the prices of (and yields on) futures contracts. Consequently, changes in market expectations can be identified by shifts in the pattern of yields on futures contracts (futures rates). Sharp declines or increases in futures rates can be identified as changes in the expected level of future interest rates. Thus, a comparison of the quotations on futures contracts at two different points in time provides information on whether market expectations have changed with regard to the future level of short-term rates. One implication of this is that it may be possible to assess the effect of a change in monetary or fiscal policy on market expectations of future short-term interest rates.

Futures Rates and Expected Spot Rates

One way of looking at the price and yield quotations on Treasury bill futures contracts in Table I is to interpret the yields on each futures contract as a market estimate of the three-month Treasury bill rate that is currently expected to prevail in each delivery month. Thus, the market's expectation on March 14, 1977, was that the three-month bill rate would be 5.23 percent in June of this year, and would increase another 126 basis points by December to 6.49 percent. In comparison, the three-month bill rate on March 14, 1977, for currently traded three-month bills, was about 4.57 percent.

However, such use of the Treasury bill futures rates is subject to some reservations. The main question is whether the futures rates are unbiased estimates of the market's expectations of future interest rates. According to the "normal backwardation" argument of Keynes and Hicks, futures prices are downward-biased estimates of expected future spot prices.5 This implies that even if future spot prices are expected to remain the same as the current spot price, the futures price will be below the expected spot price by an amount equal to a risk premium. This premium is considered to be a return to speculators for assuming the risk of possible future price fluctuations, and is larger for delivery dates which extend further into the future. This implies, in turn, that the price of the futures contract will tend to rise (the yield will fall) as the delivery date approaches, provided there is no change in market expectations.

In terms of futures markets in Treasury bills, the theory of "normal backwardation" implies that yields on futures contracts are upward-biased estimates of expected future interest rates (since prices and yields of securities are inversely related). Accordingly, the interest rate on three-month Treasury bills expected to prevail as of some future delivery date is less than the yield quoted on the futures contract for that

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4This discussion does not imply that the Treasury bill futures market satisfies the "efficient market" hypothesis. In an "efficient market", all available information is utilized immediately by traders (and potential traders), new information is available to everyone at the same time, and new information is immediately incorporated into market prices and yields. The discussion in the paper implies only that some of the available information is utilized by traders (or potential traders), and that new information which is utilized is quickly reflected in futures prices. This allows for information costs and imperfect information among market participants. For a general discussion of the "efficient market" model, see Oldrich A. Vasicek and John A. McQuown, "The Efficient Market Model," Financial Analysts Journal (September - October 1972), pp. 71-84. For a theoretical treatment, see Eugene F. Fama, "Efficient Capital Markets: A Review of Theory and Empirical Work," Journal of Finance (May 1970), pp. 383-417; or Richard Roll, The Behavior of Interest Rates: An Application of the Efficient Market Model to U.S. Treasury Bills (New York: Basic Books, Inc., 1970).

delivery date. In addition, if yields on futures contracts are higher for later delivery dates than for earlier delivery dates, it is not certain that the expected future spot rate is higher for the later delivery dates than for the earlier delivery dates. This is because a larger risk premium is included in the yield associated with the later delivery dates. Only if the difference between the yields for an earlier and later delivery date exceed the difference between their risk premia can one conclude that the expected future spot rate is higher for the later delivery date.

One implication of this line of reasoning is that gradual declines in futures rates cannot necessarily be identified as declines in market expectations of future spot rates, since the yields on futures contracts tend to fall as the delivery date approaches. However, sharp declines indicate a change in expectations, as do increases in futures rates, provided the risk premia are constant or change very little (which is generally assumed by the theory).

If these risk premia could be easily estimated, market expectations of future interest rates could be estimated from quotations on futures contracts. Unfortunately, this is not the case. In addition, other analysts dispute the "normal backwardation" argument and claim that futures prices are unbiased estimates of expected future spot prices.7 The issues surround-

6Hicks used the "normal backwardation" argument of the futures market in his development of the liquidity preference theory of the term structure of interest rates. See Hicks, Value and Capital, Chapters XI and XIII. In the literature on the term structure, market expectations of future interest rates have been examined using the implied forward rates which are embodied in the yield curve. These implied forward rates are theoretically equivalent to futures rates.


The existence of a bias in the futures rates can be tested by investigating whether, with constant expectations, the prices of futures contracts rise (yields fall) as the delivery date approaches.

### Trading Volume

Another issue bearing on the usefulness of the futures rates involves the amount of trading which occurs in each contract. Generally, it is thought that the larger the amount of trading in a security, the more representative the price and yield quotations.
Table II

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Source: International Monetary Market Division of Chicago Mercantile Exchange

will be of the market value of the security.9 In the case of Treasury bill futures contracts, this suggests that contracts with low trading volume are not representative of the market value of these contracts, and, hence, are not representative of market expectations. However, the issue is more complicated than this.

As can be seen from Table II, trading in any particular futures contract is low when it is first traded, increases over time, but then is again low as its delivery date approaches. For example, trading in the futures contract for delivery in March 1977 can be examined by reading down the appropriate column in Table II. This issue was first traded in March 1976, and the average daily volume of trading was only 7.84 contracts. By November 1976, trading increased to over 345 contracts per day. But after January 1977, with less than two months to the delivery date, trading declined below 100 contracts per day.

As the delivery date approaches, trading volume generally declines because there is greater certainty as to the spot rate will be on the delivery date. That is, traders tend to agree as to the future market value of three-month Treasury bills (their expectations become homogeneous) when the delivery date is near. Consequently, there is less risk of interest rate fluctuations to be hedged against, and less likelihood that profits can be made from trading, so that less trading occurs. In this case, the futures rates do reflect the market valuation of the contracts, even though there is little trading.

However, a lack of trading may also be indicative of a case where market participants have ill-defined expectations of future interest rates and their expectations are so diffuse that traders' bid or asked prices are not matched up with each other. In this case, there is little trading because there is great uncertainty as to the range in which the future spot rate will fall. It is possible that this case applies to the futures rates associated with contracts for delivery in fifteen to eighteen months, such as the March 1978 contract which was first traded in September 1976 (Table II).

On the other hand, when market participants have well-defined but heterogeneous expectations of future spot rates, trading activity is likely to be large. In this case, traders tend to agree as to the range in which the future spot rate will fall, but disagree as to the exact value. Market participants perceive that there is greater risk of interest rate fluctuations to be hedged against, and that profits can be made from trading. Bid and asked prices on contracts for the delivery date match up over a larger number of traders, and trading volume is larger.

Therefore, the extent to which the yields on futures contracts for particular delivery dates accurately reflect the market value of these contracts, and market expectations of future interest rates, depends upon the distribution of the expectations of traders. It is not simply a matter of the amount of trading in each contract.

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9 This line of reasoning underlies, in part, the construction of the Treasury Department's yield curves, which give greater weight to the yields of some actively traded issues.
The volume of trading also reflects on the Treasury bill futures market as a whole. The volume of trading in futures contracts compares quite favorably with the volume of trading in the spot market for Treasury bills. The total volume of trading in the Treasury bill futures market was relatively light during the first two months of trading after its opening on January 6, 1976. But beginning in March 1976, trading increased substantially to an average daily volume of about 318 contracts (Table II). With each contract representing $1 million of three-month bills, this trading represented the daily exchange of $318 million of Treasury securities in the futures market. In contrast, the average daily volume of trading by securities dealers in the spot market for all outstanding Treasury bills (approximately forty different issues) was $6.76 billion during March 1976. These figures average out to a daily volume of roughly $64 million for each Treasury bill futures market issue (five issues were traded in March 1976), compared to about $169 million for each outstanding Treasury bill issue in March 1976.

MARKET EXPECTATIONS OF SHORT-TERM INTEREST RATES SINCE JANUARY 1976

The pattern of yields on Treasury bill futures contracts since the initiation of trading on the International Monetary Market is shown on a daily basis in Chart I. Examining the movement of these yields provides some insight into the adjustment of market expectations of future short-term interest rates to new information about the state of the economy and the future supply of and demand for credit. The chart shows that the yields on all of the futures contracts being traded during any particular time period follow the same pattern of movement to a remarkable degree.

During the first quarter of 1976, market expectations of the future level of the three-month Treasury bill rate increased as the economy experienced a 9.2 percent annual rate of growth in Real Gross National Product (GNP). With the economy growing at such a rapid pace, market participants apparently anticipated a continuation of this upswing in economic activity during the remainder of the year, although not at so fast a pace. This expected strength in economic activity was translated into anticipations of increased demands for short-term credit, with a consequent rise in interest rates. During March 1976, the yield on the September 1976 futures contract was generally above 6.50 percent, while the currently traded three-month Treasury bill yielded about 5 percent.

The yields on futures contracts declined during April 1976, but by May yields had returned to roughly the same levels as were recorded in March (Chart I). During most of April 1976, newly available data indicated moderating pressures on the credit market and expectations of future levels of interest rates were revised downward. For example, the yields on the September 1976 futures contract during April were close to 6 percent, down from about 6.5 percent in March. Data on the money stock (M1) that became available in the first half of April showed that the money stock had grown at a 2.9 percent rate over the first quarter of 1976, well below the FOMC's announced target ranges for M1 growth. Most market participants apparently did not anticipate any near-term tightening in monetary policy actions, and viewed the growth of money as being consistent with a continued gradual reduction of the longer-run inflationary impact of policy actions. The preliminary GNP data available in mid-April continued to show a slowing in inflation and a strong surge in real output growth. Business loan demand at commercial banks remained weak and Treasury financing requirements were running well below earlier estimates.

Beginning in late April 1976, however, there were several developments that acted to change market expectations. On April 22, market participants became aware that there had been a very sharp surge in M1 in early April (money stock data is reported with a one-week lag). Data available in May indicated that the money stock was rising very rapidly, expanding at nearly a 17 percent annual rate in April and then at a 5.7 percent rate in May. On May 3 it was announced that the FOMC had voted at its April meeting to lower the upper band on the long-run growth of M1 from 7½ to 7 percent. The Federal Reserve moved to a more restrictive policy, and this was made apparent to market participants by a steady rise in the Federal funds rate from about 4.78 percent in the week ended April 23 to 5.02 percent in the week ended May 14. Then, at its May 18 meeting, the FOMC voted to adopt a Federal funds range of 5-5¼ percent, compared to a 4½-5¼ percent range at the April meeting. By the week ended May 28, the Federal funds rate had risen to an average of 4.94 percent.

11Ibid. Rates of growth of the money stock used in this paper are the originally reported figures, not the subsequently revised figures.
Yields on Treasury Bill Futures Contracts

January 1976 - April 1977

All yields are on a discount basis.

Source: International Monetary Market Division

Digitized for FRASER
http://fraser.stlouisfed.org/
Federal Reserve Bank of St. Louis
5.50 percent. As this new information about the course of monetary developments became available, market anticipations of future levels of interest rates returned by late May to about the same level as was recorded in March 1976.

The expected increase in credit demand failed to appear, GNP growth remained moderate, the inflation rate declined, and the unemployment rate increased during the summer of 1976. Growth of the money stock fell to about a 3 percent rate from May to September. Yields on futures contracts and the spot rate on three-month bills both declined slowly from late May until early October, when the yields on futures contracts fell quite sharply. This sharp decline was reversed in late October when yields increased almost to their early September levels. This reversal in expected yields was also associated with incoming monetary data that indicated a sharp surge in the rate of growth of the money stock. From September to October, M1 increased at a 15.5 percent annual rate.

Indicators of the strength of economic activity continued to decline during the last quarter of 1976, as did the rate of inflation, and market interest rates on all types of securities continued to decline. In the last half of November, market expectations of future interest rates declined sharply. After the surge in M1 growth during October, the money stock was little changed during November. But the Federal funds rate declined from about 5 percent in early November to about 4.75 percent in early December, which, in turn, was interpreted by market participants as indicating that the Federal Reserve had adopted a somewhat less restrictive policy. During November, yields on futures contracts fell 50 basis points or more. With pessimism about the “pause” in the economy mounting, yields on futures contracts for Treasury bills continued to fluctuate around these lower levels until the end of the year.

The increase in expected future interest rates in early January 1977 coincided with the new Administration’s announcement of a stimulative fiscal package. At the same time, data on the economic indicators for November were revised upward and a strong showing of some of the indicators for December was reported. Furthermore, monetary actions were no longer moving toward a further reduction in the Federal funds rate, contrary to the initial expectations of many market analysts. As a result, yields on futures contracts increased to their levels of mid-October through early November.

From early January through March 1977, yields on futures contracts were relatively stable. During April, when the Administration’s rebate program was cancelled and the energy program was announced, futures rates fluctuated sharply. As new information on the state of the economy and on future supplies and demands for credit becomes available to market participants, the expected future interest rates that are embodied in the yields on future contracts for U.S. Treasury bills will be revised. Movements in the levels of these yields will, therefore, provide a significant indicator of revisions of market expectations of future short-term interest rates.

**SUMMARY AND CONCLUSIONS**

The Treasury bill futures market provides a means for hedging against interest-rate risk. Speculators are allowed the opportunity of making profits in this market in return for bearing the risk of future interest rate fluctuations. In addition, futures markets provide information about the expected future pattern of prices. In doing so, indications of changes in market expectations of future short-term interest rates can be obtained. Although exact estimates of the expected level of future spot rates may not be obtainable from futures rates without adjusting for a risk premium, an approximation of the level is possible.

If it can be shown that futures rates are unbiased estimates of expected future interest rates, the data from the Treasury bill futures market could be very useful in a number of ways. Policymakers would be able to readily assess the effects of policy changes on market expectations of future interest rates. Economists and other researchers would have observable values for market expectations of interest rates, instead of having to use proxy variables for such expected rates. Analyses of the portfolio behavior of financial intermediaries, investment decisions of firms, and the term structure of interest rates are among the many areas of research which would be aided by the use of such data. In addition, analysts who forecast interest rates would be able to compare their estimates of future interest rates against the market’s expectations. Since market expectations of interest rates are an important factor in many economic relationships, the information on expectations contained in the Treasury bill futures market will be of increasing interest to businessmen, financial managers, policymakers, and other economic analysts.
Energy Resources and Potential GNP

ROBERT H. RASCHE and JOHN A. TATOM

The dramatic change in supply conditions for energy resources since 1973 had a substantial effect on the productive capabilities of the U.S. economy. Higher prices of energy resources, relative to the prices of labor and capital resources, resulted in a loss of economic capacity and higher output prices. It has been estimated that four to five percentage points of both the higher price level and reduction in national output in 1974 were due to the increased scarcity of energy resources entailed by the quadrupling of OPEC petroleum prices.1

The loss of national output because of energy market developments was a permanent loss. The energy price revision reduced the effective supply of resources available. Thus, the rate of output achievable by fully utilizing the nation’s resources, the “potential” output of the economy, was lowered.

Conventional methods of measuring the economy’s potential have focused primarily upon the availability and productivity of labor resources. More recently such efforts have also attempted to account for the availability and productivity of capital resources. Estimates of potential output which consider the relationship of only capital and labor resources to national output are not well suited to the task of accounting for the effects of changes in the availability or cost of energy resources. Nevertheless, the Council of Economic Advisers (CEA) has recently pointed to evidence which indicates that a permanent drop in the productivity of U.S. capital and labor resources may have occurred after 1973. The CEA suggests that this drop is due to the higher cost of energy resources.2

A direct route to estimating potential output, which accounts for the supplies of labor, capital, and energy resources under conditions of full utilization, is possible. Such an approach shows that a preoccupation with the supply of energy resources in measuring potential output is not important prior to 1973. Only small year-to-year changes in the relative scarcity of energy occurred before 1973. The effect of such changes was minor and capable of being captured by the trend growth of productivity of labor and capital. However, such a direct approach also demonstrates the fundamental importance of accounting for energy in measuring potential output after 1973. When energy is included in the production relationship linking resources to output, the effect of the increased scarcity of energy is seen to be of the magnitude of our earlier estimates which were based upon economic theory and more indirect evidence.

Aside from clarifying the recent performance of the U.S. economy relative to its potential, estimates of potential output which account for energy resources have important implications for economic and social prospects. Potential output measures which do not include the loss due to the change in the world energy market overstate the gains in output achievable by full utilization of resources. Consequently, such measures, in addition to endorsing impossible short-term growth possibilities, foster an inflationary bias in efforts to achieve an unattainable potential output. Also, unrealistically high estimates of potential output imply corresponding overestimates of the tax revenues associated with full resource utilization. Thus, federal budget planning tends to have a greater bias toward deficits.

THE DEVELOPMENT OF MEASURES OF POTENTIAL GNP

The Original CEA Estimates

The notion of potential GNP, the output rate produced when the economy fully utilizes its resources, was first developed by the Council of Economic Advisers in 1962.3 The original estimates of potential GNP were based on three simple statistical approaches

developed by Okun that related the unemployment rate to actual real GNP. The estimates assumed that full utilization of resources occurs when the unemployment rate for the civilian labor force is four percent, that is, the economy operated at its potential in mid-1955. The original estimates assumed that potential output grew at an annual trend rate of about 4.5 percent from 1947 to 1953, and at about a 3.5 percent rate from 1953 to 1962.

The original estimates achieved widespread recognition. The simple device of relating departures of the unemployment rate from four percent to the "gap" between actual and potential output facilitated the popular discussion of both economic goals, such as full employment and growth, and fiscal policy. With regard to the latter, the notion of a high-employment Federal budget was developed and used to indicate the state of the budget deficit or surplus under high-employment economic conditions as well as the magnitude of fiscal efforts required to move the economy to a four percent unemployment rate.

Since these original estimates, the CEA has recognized that various forces, particularly demographic factors, can change the trend rate of growth of resources and, hence, potential output. Consequently, the CEA has from time to time adjusted the trend rate of growth used to update their data series for potential output. From 1952 through 1962, the CEA uses the 3.5 percent trend rate of growth derived by Okun. This trend rate was raised to 3.75 percent for the period from 1962 through 1968 and further increased to four percent from 1969 through 1975. Because of a slowdown in the rate of growth of the labor force, the CEA reduced the trend rate of growth of potential GNP after 1975 to 3.75 percent. This series is referred to below as the "old" CEA estimate and is shown in Chart I along with actual GNP.

Okun indicated in his original work that his analysis skipped over important links between changes in the unemployment rate and output, and in an often quoted passage he concluded:

Still, I shall feel much more satisfied with the estimation of potential output when our data and our analysis have advanced to the point where the esti-
mation can proceed step-by-step and where the capital factor can be taken explicitly into account.\(^6\)

Since 1962 several studies have attempted to improve upon the original work. The major efforts attempted to account for capital resources and for the interaction between actual output and prospective potential output. The major development has been to use an approach based upon an aggregate production function.\(^7\) However, until recently no serious problems have been detected with the old CEA estimates.\(^8\)

### The “New” CEA Potential Output Series

More recently, studies of potential output have indicated some major departures from old estimates. In addition to the slowdown in the long-term growth of the labor force pointed out by the CEA in the fall 1976 revision of the growth trend, a study by Data Resources, Inc., suggests a further slowdown since 1973 because of a substantial decline in the growth of the capital stock.\(^9\) More importantly, the CEA itself has pointed out an apparent slowdown in productivity growth since 1966. Clark has developed a new potential output series for the CEA which is based, to an extent, on production function estimates rather than simple trends.\(^10\) These new estimates imply a growth rate of potential output of about 3.5 percent in the late 1960s and early 1970s. These new estimates are in agreement with projections made in 1972 by William Nordhaus.\(^11\)

In two respects the new CEA series on potential output represents a major departure from the methods used to compute the old series. First, potential output now is viewed more as high-employment output rather than being linked to a four percent unemployment rate. The new CEA estimates are based on explicit considerations of participation rates and differential high-employment unemployment experiences of different age-sex groups. The high-employment benchmark of a four percent civilian labor force unemployment rate in mid-1955 is preserved, but the new series is based on explicit estimates of the revision in the high-employment benchmark over time due primarily to changes in the composition of the labor force. The second major departure is an attempt to account more explicitly for capital resources in the estimation of productivity and potential output. However, the new estimates of the CEA do not take into account a further one-time reduction in productivity and potential output which their analysis indicates occurred in 1974 and which they suggest may be a permanent change due to the energy price shock.\(^12\)

A comparison of the new and old series is presented in Chart II for the period 1952-1976. Until 1967, the two CEA potential output series are very similar. The new CEA estimates show potential output to be about one percent lower from 1952 to 1967, but growing at roughly the same rate. After 1967 the new estimates fall short of the old series by a growing amount. By 1976 the new estimate of $1363.6 billion is only 95.9 percent of the old estimate of $1421.2 billion.\(^13\) The bulk of the $57.8 billion reduction is attributed to a slowdown in the growth of labor productivity and an increase in the full-employment unemployment rate.

As noted above, the CEA has suggested that productivity fell further in 1974, so that by 1976, potential output may be $30 billion lower than their own new estimates. These new estimates, like those of Data Resources, Inc., mentioned above, assume a

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\(^{6}\)Okun, “Potential GNP,” p. 104.


\(^{8}\)For example, see the discussion by George M. vonFurstenberg, “Comments on Estimating Potential Output for the U.S. Economy in a Model Framework,” Achieving the Goals of the Employment Act of 1946—Thirtieth Anniversary Review, U.S. Congress, Joint Economic Committee, 94th Cong. 2nd sess., December 3, 1976, pp. 26-28. He points out that more elaborate “supply-oriented models” are valuable for improving understanding, but estimates from them are not “demonstrably more reliable” than the old official estimates. He also notes that the usefulness of the old CEA potential output estimates “would be unaffected by anyone showing, for instance, that potential is consistently one percent larger or smaller than officially estimated” (p. 28).


\(^{12}\)While the Economic Report discusses the new estimates, neither the old nor new series have been published in the monthly publication of the Bureau of Economic Analysis, Business Conditions Digest, since October 1976.

\(^{13}\)See CEA, Economic Report, 1977, p. 55. All potential output measures are in constant (1972) dollars throughout this article.
Cobb-Douglas production function with only labor and capital resources and assume output elasticities of one-third for capital and two-thirds for labor. Thus, neither estimate is able to capture fully changes in productivity of labor and capital resources due to reductions in potential energy usage associated with a higher relative price of energy resources.

The production-function approach to the estimation of potential output taken in this article accounts explicitly for energy resources. The potential output measures draw heavily upon the recent work involved in the new CEA measures of potential output, specifically by using their estimates of the potential labor force and the full-employment unemployment rate.

One recent study, that of Eckstein and Heien (E-H), has attempted to account for energy effects on potential output through the aggregate production function.14 The E-H results indicate, however, that in recent years potential output is much higher than the old CEA estimates. While the methodology used in the E-H study is similar to that used here, the conclusions are markedly different. These differences result from serious data problems and a specification error in their demand for energy. Since their study has such a similar methodology and reaches such different results, a full critique is contained in Appendix I.15

ACCOUNTING FOR ENERGY IN AN AGGREGATE PRODUCTION FUNCTION

The first step in a production-function approach to measuring potential output is the estimation of an

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15Another study which includes energy price developments in an estimate of potential output is that by Jacques R. Artus, "Measures of Potential Output in Manufacturing for Eight Industrial Countries, 1955-78," *International Monetary Fund Staff Papers* (March, 1977), pp. 1-35. Like Clark's study he finds an energy price impact using a dummy variable approach instead of explicitly incorporating the energy price. Since his study includes seven countries he is forced by data limitations to impose several arbitrary constraints which raise serious questions about the meaningfulness of his coefficient estimates. Relaxing the constraint that the effect is the same across countries, his estimate of the energy price impact is that U.S. potential manufacturing output fell 2.7 percent in 1974 which is below both Clark's estimate of 4.2 percent for the private business sector and our earlier estimate of five percent which is confirmed below. Ignoring the other constraint problems, it may be noted that his estimate is not significantly different from ours given its relatively large standard error.
aggregate production function. The approach taken here follows the usual practice with one major exception: energy resources are considered as an integral part of the production function. This is in contrast to the usual practice of estimating the functional relationship between output and only labor and capital resources. The latter approach implicitly assumes that changes in the stock and flow of energy resources are captured by movements in the capital stock and need not be explicitly taken into account.

The measure of output for which a production function is estimated is the output of the private business sector. Real GNP includes, in addition to the output of the private business sector, gross output originating in the rest of the world, the output of the general government sector, output imputed to owner-occupied dwellings, and output of households and nonprofit institutions. For estimating potential real GNP these components of actual GNP are simply added to potential real output of the private business sector.

Actual real output in the private business sector depends upon the employment of capital and labor services as well as energy resources. The production function may be written as

\[ Y = A e^{\alpha} L^{\beta} K^{\gamma} E^{\rho} \]

where \( Y \) is output, \( L \) is labor measured in manhours, \( K \) is the effective flow of capital services, \( E \) is the flow of energy resources, and \( t \) is time. The other terms in equation (1) are estimated statistically. The \( A \) term is essentially a scaling factor, \( r \) is the trend rate of growth of output due to technological change, and \( \alpha, \beta, \gamma \) are the output elasticities of the respective inputs. The estimated production function was restricted by requiring that the sum of the exponents \( \alpha, \beta, \gamma \) equal unity. The basic implications of such a "Cobb-Douglas" production function are constant returns to scale and partial elasticities of substitution of unity.\(^{16}\)

The output and manhours data for the private business sector are those prepared by the Bureau of Labor Statistics of the U.S. Department of Labor. The effective services of capital are found by multiplying the Federal Reserve Board index of capacity utilization times the capital stock in place at the beginning of each period.\(^{17}\) The annual capital stock measure is the constant dollar (1972) net stock of fixed nonresidential equipment and structures.\(^{18}\) A comparable data series on energy use in the private business sector could not be found. However, the rate of energy use in the private business sector is presumably that demanded and the demand for energy is determined completely by the production function and the relative price of energy.

If firms in the private business sector maximize economic profits, they employ energy at a rate where the value of the additional product obtained from employing more energy equals its price. The demand for energy from equation (1) is

\[ E = \gamma Y \left( \frac{P_E}{P_B} \right)^{-1} \]

where \( P_E \) is the price of energy and \( P_B \) is the price of output of the private business sector.\(^9\) Equation (2) can be used for the energy input in the production function so equation (1) may be found by estimating

\[ Y = (A^* e^{\alpha} L^{\alpha} K^{\beta} P_B^{\delta})^{1/\gamma} \]

where \( A^* \) is another scaling factor and \( P \) is the relative price of energy \((P_E/P_B)\). The relative price of energy is measured by the ratio of the wholesale price index for fuel, related products, and power to the implicit price deflator for the output of the private business sector.

The credibility of the assumed Cobb-Douglas production function is, of course, purely an empirical matter that can be subjected to statistical testing. The assumption implies relatively high price and output elasticities of demand for energy and unit partial elasticities of substitution between energy and capital

\(^9\)In a previous paper, "The Effects of the New Energy Regime," we discussed the possible biases of the FRB capacity utilization index in recent years as a result of changes in the relative price of energy, when it is viewed as a measure of utilization of economic capacity. In the present context, we need a measure of utilized capital. When this index is viewed as such a measure, there is no reason to believe that the change in the relative price of energy has introduced a systematic measurement bias.


\(^{19}\)The marginal product of energy from equation (1) is \(\gamma Y/E\), so the profit-maximizing employment of energy occurs where \(P_E = (\gamma Y/E) P_B\).
or labor. There is, however, some evidence that these properties apply to the U.S. economy. An output elasticity of demand for energy of unity in the long run for at least the United States, Japan, and Western Europe is supported by a number of studies. Using cross-sectional data and the trans-log production function, Griffin and Gregory have demonstrated that for nine industrial nations the production function has partial elasticities of substitution of energy for capital and labor that are constant and unity. Most importantly for the purpose at hand, the assumption of a Cobb-Douglas production function cannot be rejected with the data examined.

Recent studies of productivity suggest that in estimating an aggregate production function it is important to account for qualitative changes in manhours and for productivity differences in capital due to the increasing importance of mandated pollution-abatement capital expenditures. Attempts to control for skill differences by including variables for the composition of the labor force by age were unsuccessful except for the 16-19 age group; a negative effect of the share of the latter group on productivity was not statistically significant when the estimation was adjusted for autoregression. Clark's gross capital stock data are adjusted for pollution-abatement capital. Use of his series produced results essentially identical to those found using the gross nonresidential stock of business capital (constant 1972 dollars). Thus, no attempt is made to adjust the net nonresidential stock of business capital for pollution-abatement capital.

The production function (3) estimated with annual data for the period 1949-75 is given in logarithmic form in Table I. The equation was estimated with the constant-returns-to-scale restriction imposed by taking

\[ \ln Y = 1.7134 + .7371 \ln L + .2629 \ln K \]

The estimate of the output elasticity of labor in Table I is very close to the usual estimate of labor's share of income as well as being approximately equal to labor's average share of cost in the private business sector over the period of estimation. The average share of labor in the private business sector over the sample period is 66.37 percent. A test for the differences between the estimated output elasticity and the sample period average labor share yielded a t-value of 0.2914. Thus, the hypothesis that the estimated output elasticity of manhours is equal to labor's share cannot be rejected.

Since the relative price of energy changed dramatically in 1974 and 1975, the production function in

\[ F = .96 \text{ D.W.} = 1.45 \]

\[ \hat{\rho} = .63 \]

Values in parentheses are t-statistics.

Table 1

An Aggregate Production Function with Energy (Annual Data 1949-75)

\[ \ln Y = 1.7134 + .7371 \ln L + .2629 \ln K \]

(11.71) (12.01) (4.28)

\[ -.1363 \ln P + .0185 t \]

(-5.66) (9.67)

\[ R^2 = .96 \]

\[ S.E. = .0093 \]

\[ D.W. = 1.45 \]

\[ \hat{\rho} = .63 \]

The estimated standard error of the estimate of \( \gamma \) is 2.12 percent.

The estimates of the output elasticities of the production function, based on the equation in Table I, are presented in the Table II. The output elasticity of the energy resource is 12 percent which is consistent with the Griffin and Gregory estimate of the cost share of energy and energy price elasticity of demand for capital. The latter estimates have been used to show that capacity in manufacturing fell five percent in 1974 due to the 45.3 percent rise in the nominal price of energy from the end of 1973 to the end of 1974. The estimate also supports the assumption that the manufacturing result is representative of the effect of the energy price change on the private business sector. The estimated standard error of the estimate of \( \gamma \) is 2.12 percent.

\[ \hat{\rho} = .63 \]

Values in parentheses are t-statistics.

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per year accounts for 87 percent of its variation with time trends and capital. For example, from 1948 to 1970 a trend decline of the relative price of energy of 1.33 percent per year accounts for over 95 percent of its variation with a standard error of two percent.

The production function estimates can be used to estimate potential output in the U.S. economy when supplemented with assumptions concerning the full-employment availability of resources. The stock of capital available during a period is essentially the same regardless of whether the economy operates at its potential. The utilization rate of capital, however, varies with economic conditions. Consequently, estimates of potential output for the private business sector and the economy as a whole requires some estimate of the utilization rate that would prevail at potential output. Quarterly estimates of the Federal Reserve Board index of capacity utilization in manufacturing since 1948 indicate that the 87.7 percent utilization rate of capital achieved in late 1973 has been exceeded in only two prior peak periods, during the Korean War and the Vietnam War, when it was about 90 percent. During mid-1955, a benchmark year for original studies of potential output,
the index was 87.5 percent. This latter rate is used here as the assumed full-employment capital utilization rate.

The flow of manhours at the potential output rate depends upon both the size of the "potential labor force" and the supply of hours per worker at potential output. Clark's recent study provides annual estimates of the potential civilian labor force. The estimates are based upon the population and labor force participation rate of each of eight age-sex groups adjusted for cyclical effects. Clark has also estimated a full-employment unemployment rate annually since 1948 which is equivalent to a four percent unemployment rate in 1955. These estimates are based upon the relationship between the unemployment rate for each of the eight age-sex groups and: 1) the unemployment rate of adult males (age 25-54) and 2) the relative size of the potential group in the potential labor force. An annual series for potential civilian employment is obtained by adjusting the potential labor force for the full-employment unemployment rate. Potential employment in the private business sector in each period is the difference between potential civilian employment and actual employment outside the private business sector, principally in government.

Hours per worker in the private business sector at potential output is estimated in a fairly standard manner. Hours per worker varies cyclically as well as secularly. Hours per worker at potential output, adjusted for Clark's full-employment unemployment rate, is estimated using the postwar relationship in Table IV, which treats hours per worker as a function of the unemployment rate and a time trend. Potential manhours is the product of the estimated potential hours per worker and potential employment in the private business sector.

The relative price of energy at potential output is assumed to be the actual relative price. Until 1974 it is conceivable that moving from a smaller output to potential output in any period would have raised this relative price. However, since any change of this type would have probably been quite small given the small variance in this relative price in the postwar period through mid-1973, and since the coefficient of the relative price is not large, it is unlikely that the assumption has any noticeable impact on the estimates of potential output.

The production function and the assumptions above provide an estimate of potential output in the private business sector. Potential real GNP is found by adding the actual component of output outside the private business sector. The annual estimates of potential real GNP from 1952 to 1976 are shown in Chart III along with the old CEA series. Unlike both the new and old estimates of the Council of Economic Advisers, the series is not smoothed. The average annual rate of growth of the series from 1952 to 1975 is 3.4 percent. This is slightly lower than the 3.6 percent average rate of growth in the new CEA series or the 3.7 percent in the old series for the same period.

The estimate of potential output is virtually identical to the old CEA estimates in their benchmark year 1955 as well as in 1969-70. Chart IV shows the ratio of the estimated potential GNP to the old CEA measure of potential output. Except for the early and mid-1950s and 1969-70, the old CEA estimates show the economy with greater potential than the estimates here. The chart indicates that the old CEA measure grows more rapidly in the late 1950s and early 1960s, but that this is compensated for by a lower estimate of potential output growth in the late 1960s. Chart IV presents estimates of potential output along with the old CEA series.

The table presents estimates of potential output in the private business sector for the years 1948-75. The estimate of potential output is virtually identical to the old CEA estimates in their benchmark year 1955 as well as in 1969-70. Chart IV shows the ratio of the estimated potential GNP to the old CEA measure of potential output. Except for the early and mid-1950s and 1969-70, the old CEA estimates show the economy with greater potential than the estimates here. The chart indicates that the old CEA measure grows more rapidly in the late 1950s and early 1960s, but that this is compensated for by a lower estimate of potential output growth in the late 1960s. Chart IV presents estimates of potential output along with the old CEA series.

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IV also indicates that, according to our estimates, a four percent trend rate of growth is slightly too high for the period 1969-71 and about right for 1971-73. After 1973, the ratio plummets as the old trend-based estimates of potential output are unaffected by energy developments.
As indicated in Chart II, the new CEA measures of potential output are about 99 percent of the old measures until 1967. Thus, the new CEA series shows potential output to be smaller than the estimates here from 1952-59 and from 1968-73. The new official CEA estimates do not account for energy price developments so they are higher than the production function estimates for 1974-75. However, when the additional productivity shift discussed by the CEA is taken into account, their new estimate of potential output for 1974 and 1975 is not much different from those presented in Chart III.

A primary difference, besides excluding energy considerations, between the new CEA potential output series and that presented in Chart III is a productivity slowdown in 1967. The new CEA series includes such a slowdown and it is estimated that the trend rate of growth falls 25 percent after 1966. The timing of this shift appears to be arbitrary and its size appears to be quite large given the reasons cited. Nonetheless, such a shift is statistically significant when a variable intended to capture such an effect is added to the equation in Table I. Moreover, the size of the reduction in the trend rate of growth agrees with the estimates of the CEA. The estimated equation is presented in Table V. It may be noted that the equation implies a significant output elasticity of energy of 9.8 percent and an output elasticity of manhours of 66.8 percent. Given the size of the standard errors of the coefficients, it does not appear that the inclusion of the productivity shift parameter, T2, significantly affects the results indicated in Tables I and II. The only major differences between the equation in Table V and the equation in Table I are the differences in the trend rate and the slight improvement in the standard error.

For comparison purposes, a potential output series was estimated as before using the production function in Table V. The comparison is essentially the same as that discussed above without the shift term T2. The ratio of the estimated potential output, with and without the slowdown in productivity growth, to new CEA potential output is shown in Chart V. The new CEA estimates are lower than our estimates of potential output before 1959 and in 1968-73. Like the old CEA estimates, the new CEA estimates indicate a higher rate of growth of potential output until the mid-1960s and a lower rate of growth of potential output from 1965-69. The new CEA rate of growth of potential output from 1969-73 is in agreement with the energy based estimate. Finally, like the old CEA estimates, the new CEA estimates show a higher rate of growth of potential output in 1974-75.

THE IMPLICATIONS OF NEW ESTIMATES OF POTENTIAL OUTPUT

Regardless of the historical pattern of the alternative estimates of potential output, the new CEA estimates and those presented here have similar implications for the recent and near term performance of the economy. Table VI shows the potential output measures for 1973-76 from the old series, the new series, and those estimated using the equation in Table I and shown in Chart III. Both of the new estimates show that the economy was much closer to potential output in 1973 than the old CEA series indicates. More importantly, both new series show a substantially slower growth of potential output in recent years, compared to the old series and, thus, a substantially smaller gap between actual and potential output in 1976.

Our estimate of potential output also supports the CEA’s recent suggestion that energy price develop-

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39 The conclusions from Table VI would be unaffected by using the production function in Table V since the potential measures for 1973-76 are essentially the same on either basis.
ments reduced potential output by an additional $30 billion by 1976. When this effect is subtracted from the new CEA estimate for 1976, the result is within one percent of our estimate of potential output.

Our estimate of potential output suggests that in 1975, the economy failed to produce about 7 percent of its potential output due to the recession. In contrast the old and new CEA estimates suggest that the gap was about 13 percent and 10 percent, respectively. More importantly, the gap fell to 4.5 percent of potential output in 1976 while the CEA estimates indicate it only fell to 11 or 7 percent of potential output. On the basis of the old CEA series, the worst loss of potential output, prior to the 1973-75 recession, occurred in 1958 when the gap was about 6.5 percent of potential. Thus, both CEA estimates imply the economy performed very poorly relative to potential output in 1976. In contrast, a 4.5 percent shortfall of actual from potential output is about the same as the performance indicated by our historical series for 1960-61 or 1971.

The gain in output to be achieved by moving to a fully-employed economy is substantially smaller than

<table>
<thead>
<tr>
<th>Year</th>
<th>Old CEA</th>
<th>New CEA</th>
<th>Production Function (Table I)</th>
<th>Actual GNP</th>
</tr>
</thead>
<tbody>
<tr>
<td>1973</td>
<td>$1265.4</td>
<td>$1228.2</td>
<td>$1249.2</td>
<td>$1235.0</td>
</tr>
<tr>
<td>1974</td>
<td>1315.9</td>
<td>1271.7</td>
<td>1257.8</td>
<td>1214.0</td>
</tr>
<tr>
<td>1975</td>
<td>1368.6</td>
<td>1316.9</td>
<td>1283.8</td>
<td>1191.7</td>
</tr>
<tr>
<td>1976</td>
<td>1421.2</td>
<td>1363.6</td>
<td>1324.6</td>
<td>1264.6</td>
</tr>
</tbody>
</table>

Table VI Three Measures of Potential Output (Billions of 1972 Dollars)
either the old or the new CEA measures indicate. Attempts to expand demand and production to such unattainable levels in the near term would consequently accelerate inflation. The period of time over which output may grow at a given rate faster than the growth rate of potential output is correspondingly smaller. The rate of growth of potential output will constrain actual output growth much earlier than the old measure suggests. Also, at the output rate achieved at full employment, Federal tax receipts and budget surpluses will be smaller than the higher measures of potential indicate. Thus, a goal of a balanced budget at full employment will require more effort than either of the CEA estimates indicate.

CONCLUSIONS

Since 1962 estimates of potential output have become popular and important sources of information for policy formulation. The early estimates, and until recently the official estimates, focused upon labor resources only. New estimates by the CEA have attempted, to some extent, to account explicitly for the importance of capital resources and a production function. The CEA has also suggested that energy developments are an important factor affecting the productivity of fully-employed resources.

Using a production function which accounts explicitly for capital and energy resources, an alternative measure of potential output has been developed. The production function estimates support the argument that the new energy regime imposed in 1974 permanently reduced potential output by about four percent. The production function estimates show that failure to account for energy prior to 1973 is not critical, but that serious inconsistencies arise when the sample period is extended to include recent years.

Until 1973 the historical series for potential output developed here tends to conform more to the old CEA series than the new series. After 1973, however, the new CEA estimates adjusted for the magnitude of their suggested decline in productivity are very close to our estimates. Thus, while our estimates cast some doubt on the historical accuracy of the new CEA estimates, they support the CEA's suggestion that energy price developments after 1973 reduced potential output.

The implications of the new CEA estimates and those presented here are of great significance for the full-employment and growth prospects of the economy. Attempts to achieve an unattainable potential output rate through stimulative policy will not only fail, but will add to inflationary pressures. Also, there is little prospect for an extended period of growth at rates higher than the rate of growth of potential output (about 3.5 percent per year). The gap between potential and actual output will tend to close within two years, even with the moderate growth of actual output achieved in 1976. Finally, at full employment, existing tax and spending policies will result in a much larger budget deficit than higher measures of potential output indicate.

APPENDIX I

An Analysis of the Eckstein-Heien Model for Determining Potential Output

In a recent study for the Joint Economic Committee, Eckstein and Heien (E-H) have estimated an annual

The first difference involves the choice of data series. E-H choose to study the private nonfarm sector of the economy. This differs from the private business sector as defined in the text, in that the E-H measure excludes the farm sector of the economy, and includes the imputed output to owner-occupied housing and output originating in households and non-profit institutions. They also choose to use raw materials as the third factor of production in their estimated production function, in contrast to the energy input concept employed above. In practice this difference should not be too important, since 88 percent of the weight in their Laspeyres index of raw materials comes from the crude oil, refined petroleum products, natural gas and coal components of their index. The wholesale price index of energy used above measures just these components plus electrical power, so the correlation of the two input measures should be very high.

E-H estimate a three factor Cobb-Douglas production function on annual data from 1950-74. The estimated output elasticities in their function can be compared with those implied by the production function which is reported above. All three estimated elasticities are essentially identical in both studies. In addition, the estimated coefficient on the time variable is almost exactly the same in both equations. The differences in the conclusions of the two studies, therefore, cannot be attributed to differences in the underlying production function, the central relationship in both analyses.

E-H present a 12 equation model, while the analysis above explicitly involves only one equation. For the purposes of constructing potential output, the elaboration in their 12 equations is somewhat misleading. They use the assumption that four percent unemployment is the appropriate rate of labor force utilization at which to construct potential output. With this assumption, their model can be characterized by three distinct blocks: 1) an employment block consisting of the labor force participation equations and the various identities defining employment, labor force and unemployment, 2) a wage-price block consisting of the equations for the wage rate in the private nonfarm economy and the price of output in the private nonfarm economy, and 3) an output block consisting of the production function, a derived demand equation for raw materials, and an equation for the average hours per worker.

Under the assumed ‘full-employment’ conditions, the employment block is completely independent of the rest of the model. The size of the male labor force is expressed solely as a function of exogenous variables, so it is also an exogenous variable for purposes of the model. The female labor force is a function of exogenous variables, other variables within the employment block of the model, and lagged variables from other blocks of the model. The various identities in this block relate variables defined within the block to exogenous variables. Therefore, it is possible to solve this subset of their equation system for the total private nonfarm employment as a function of only exogenous variables. Private nonfarm employment can affect variables in both the wage-price block and the output block.

The wage-price block is affected by two exogenous variables, the price of raw materials and the full-employment unemployment rate. It is also affected by the employment block and the output block, since these parts of the model determine employment and output which affect unit labor costs. Unit labor costs are specified as an important influence in the determination of private nonfarm wages.

The output block is affected by the exogenous capital stock and exogenous capacity utilization rate. It is affected by the employment block through employment in the private nonfarm sector which enters into the aggregate production function. Furthermore, the only link between the wage-price block and the output block is through the relationship for the average number of hours per worker, which depends on the real wage rate. This relationship is not particularly strong, since the elasticity of the average number of hours per worker with respect to the real wage rate is only .2, but it explains why E-H obtain a positive relationship between raw materials prices and potential output.

In the E-H model, an increase in raw materials price directly affects the price of output in the nonfarm sector. A higher price level in turn causes higher wages, but the increase is less than proportional, so the real wage rate falls in response to the increase in raw materials prices. Real wages have a negative impact on the average number of hours per worker, so hours per worker rise in response to the increase in raw materials prices. Total private sector employment in the model is exogenous at potential output as discussed above, so total manhours rise in response to the increase in raw materials prices. The net effect is an elasticity of real output with respect to raw materials prices in the E-H model of .02. The small magnitude of this elasticity illustrates the weakness of the interrelationship of the price-wage equations of the model with the output equation through the average hours equation.

If E-H had assumed, as do the authors of other studies of potential output, a fixed number of hours per person at full employment, then the link between the wage-price block and output block in their model would be broken. Their potential output model would then consist only of two equations; the production function and the demand for raw materials equation, supplemented by exogenous assumptions on the magnitude of manhours supplied at potential output. Under these circumstances their analysis would imply that there is no effect of changes in raw materials prices on potential output. In practice, their analysis effectively implies such a conclusion since the price elasticity reported above is so close to zero.

The two equation model which is so closely approximated by the E-H model is exactly the two equation model which is implicit in the analysis presented above. The aggregate production function, with the relative price of energy as one of the right hand side variables, is derived by substituting the demand equation for energy under the assumption that the real price of energy
inputs is exogenous. Recall that the estimates of the production function parameters are essentially the same for the two studies. Therefore, the difference in the results obtained must be attributable to differences in the explicit or implicit demand functions for energy inputs.

The problem with the E-H model is that the demand functions for both labor and raw material inputs are misspecified. Such demand functions normally would be expected to be consistent with the first-order conditions for cost minimization and/or profit maximization. In the case of the Cobb-Douglas production function, this implies that the input demand functions must be log-linear. Yet both the demand function for raw materials and the demand function for labor services in the E-H study are specified as linear functions. This probably accounts for the insignificance of the estimated coefficient of the relative price term in the raw material demand equation which E-H report in the text, but not in the equations of the model.

The approach used in this study implicitly assumes that both the output elasticity and the price elasticity of the demand for energy are one, and that the functional form of this equation is log-linear. If this were not the case, then the output elasticities derived from the production function parameter estimates should be biased. Three pieces of evidence suggest that this is not the case. First, the estimated output elasticity of labor services conforms quite closely to the share of labor in total income as it should under the constant-returns-to-scale restriction. Second, the estimated output elasticity of energy inputs conforms almost exactly with the estimates from cross-section time series data of several countries, including the United States obtained by Griffin and Gregory. Third, as mentioned above, the estimated output elasticity of energy (as well as of other resources) obtained in this study are almost identical to those obtained by E-H even though they used a measure of the quantity of raw materials input in estimating the production function directly.

**APPENDIX II**

Equation (2) constrains both the output and price elasticities of energy demand to unity. Consider the unconstrained hypothesis for the energy demand curve:

\[ \ln E = \delta_0 + \delta_1 \ln Y - \delta_2 \ln (P_E/P_B) + \epsilon \]

If this is substituted in the Cobb-Douglas production function:

\[ \ln Y = a + \alpha \ln L + \beta \ln K + \gamma \ln E + u \]

where \( \alpha + \beta + \gamma = 1 \), the result is:

\[ [\ln Y - \ln K] = \beta_1 + \beta_2 [\ln L - \ln K] + \gamma \epsilon + u \frac{\gamma \epsilon + u}{1 - \delta_1 \gamma} + \beta_3 \ln (P_E/P_B) + \beta_4 \ln K + \frac{\gamma \epsilon + u}{1 - \delta_1 \gamma} \]

where

\[ \beta_1 = \frac{a + \delta_0 \gamma}{1 - \delta_1 \gamma} \quad \beta_2 = \frac{\alpha}{1 - \delta_1 \gamma} \]

\[ \beta_3 = \frac{-\gamma \delta_2}{1 - \delta_1 \gamma} \quad \beta_4 = \frac{-1 + \alpha + \beta + \delta_1 \gamma}{1 - \delta_1 \gamma} \]

Therefore, if the output elasticity of energy demand, \( \delta_1 \), were not unity, the specification which has been estimated would have an omitted variable, \( \ln K \), which would be correlated with at least one of the included regressors, \( \ln (L-ln K) \), so all of the estimated regression coefficients (\( \beta \)'s) would be biased.

If the price elasticity of energy demand, \( \delta_2 \), is not unity, then the estimated regression coefficients (\( \hat{\beta} \)'s) are not biased, but the output elasticities which we have derived from the regression coefficients are biased. Our estimates of the output elasticities for labor and energy are \( \alpha^* = \beta_2/(1 - \beta_3) \) and \( \gamma^* = \beta_3/(1 - \beta_3) \), respectively. The unbiased estimates of these output elasticities are:

\[ \hat{\gamma} = \gamma^* \left[ \frac{1}{1 + (\gamma^* - 1)(1 - \beta_3)} \right] \quad \text{and} \quad \hat{\alpha} = \alpha^* \left[ \frac{1}{1 + \gamma^* \left( \frac{1 - \delta_2}{\delta_2} \right)} \right] \]

Consequently, if \( \delta_2 < 1 \), our estimate of the output elasticity of energy is biased downward and our estimate of the output elasticity of labor is biased upward. The consistency of our estimates of the output elasticities with estimates from other sources and the consistency of the output elasticity with the labor share data, suggests that biases from these sources are not substantial. Even if the output elasticities were biased because the price elasticity of energy demand was less than unity, the biases would not affect our potential output computations, since these are based on the unbiased estimated regression coefficients (\( \hat{\beta} \)'s).
A quarterly series for potential GNP can be constructed using the same method and data when some additional assumptions are made concerning the data. The principal data problems involve quarterly estimates of the capital stock and potential employment or manhours.

Quarterly data on the stock of capital are found by prorating the annual year-end changes in the net stock of fixed nonresidential equipment and structures over quarters using quarterly rates of investment in nonresidential fixed investment as the weights. Clark’s annual data on the potential labor force are assumed to be for the second quarter of each year and a linear interpolation is used for other quarters. To find potential manhours, a quarterly estimate of hours per worker is obtained such as that contained in Table IV. The quarterly potential hours per worker is found by using Clark’s full-employment unemployment rate for the respective years in the equation

\[ \ln HPW = .8120 - .0033 U - .0010 t \]

which is estimated for the period from the second quarter of 1948 through 1975.

The quarterly production function comparable to the annual estimate in Table I, (II/1948-IV/1975) is

\[ \ln Y = 1.5974 + .7192 \ln L + .2808 \ln K \]

\[ = .1164 \ln P + .0045 t \]

The estimated coefficients are essentially the same as for the equation in Table I. The estimated output elasticities and trend growth term are (standard errors in parentheses)

\[ \hat{\alpha} = 64.4\% (3.08\%), \hat{\beta} = 25.2\% (3.08\%), \]

\[ \hat{\gamma} = 10.4\% (1.85\%), \hat{\tau} = .4\% (.03\%). \]