Technology Adoption and Leapfrogging: Racing for Mobile Payments

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Abstract

Paying with a mobile phone is a cutting-edge innovation transforming the global payments landscape. Some advanced economies like the U.S., however, are lagging behind in mobile payment adoption. We construct a dynamic model with sequential payment innovations to explain this puzzle, which uncovers how advanced economies’ past success in adopting card-payment technology holds them back in the mobile-payment race. Our calibrated model matches the cross-country adoption patterns of card and mobile payments and also explains why advanced and developing countries favor different mobile payment solutions. Based on the model, we conduct several quantitative exercises for welfare and policy analyses.

Keywords: Technology Adoption, Leapfrogging, Payments System, FinTech

JEL Classification: E4, G2, O3

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1 Introduction

The payments system is an essential financial technology infrastructure of the aggregate economy. With the successful launch of general-purpose credit cards in the late 1950s and debit cards in the mid-1980s, the United States has been one of the leading countries in deploying card payment technologies. However, the United States is falling behind in adopting the recent mobile-phone-based payment innovation (henceforth, “mobile payment”).

Kenya is an early success story for mobile payment adoption. Within four years after being launched in 2007, mobile payment has been adopted by nearly 70% of Kenya’s adult population (Jack and Suri, 2014). While the mobile payment technology in Kenya relies on Short Message Service (SMS), China has introduced a mobile payment innovation based on smartphones and QR (Quick Response) codes which experienced explosive growth of usage in recent years. In 2017, a total of 276.8 billion mobile payment transactions were made in China, equivalent to 200 transactions per capita.\(^1\)

In contrast, the United States appears to be lagging in mobile payment adoption. To illustrate, Figure 1 compares the adoption rates of card and mobile payments around 2017 in three countries: Kenya, China, and the United States. Figures 1A and 1B report the percentage of the adult population (age 15 and above) having a debit card and using a mobile payment service, respectively.\(^2\) As shown by the figures, while the United States boasts a much higher card payment adoption rate, it has been significantly surpassed by Kenya and China in mobile payment adoption.

This has raised concerns by the press, business leaders, and policymakers about the efficiency and innovativeness of the U.S. payments system. With a headline of “China is out-mobilizing the United States,” the Wall Street Journal (2018) was impressed by how “Chinese consumers are adopting mobile payments in a way that is making U.S. tech companies green with envy.”\(^3\) Apple’s CEO, Tim Cook, noted in a speech that China outdid the United States in the development of mobile payment technology.\(^4\) Leaders

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2. Sources: Global Financial Inclusion (Global Findex) Database of the World Bank, and eMarketer. See Appendix I for the data details.
of the Federal Reserve System recognized “that the U.S. retail payment infrastructure lags behind many other countries” and “the gap between the transaction capabilities in the digital economy and the underlying payment and settlement capabilities continues to grow.”\textsuperscript{5}

These observations and concerns lead to relevant questions: Why did developing countries like Kenya and China lag in adopting card payments but leapfrog in adopting mobile payments? Has the United States lost its leadership in the payment area? Should the U.S. government implement policies to boost mobile payment adoption?

This paper addresses these questions. In doing so, we first compile a novel dataset to uncover the general adoption patterns of card and mobile payments across countries. The data shows that the overtaking in mobile payment adoption is a systematic pattern between developing countries and advanced economies, beyond just Kenya, China, and the United States. Moreover, the adoption rate of mobile payment shows a non-monotonic relationship with per capita income: increasing in low-income countries, decreasing in middle-income countries, and increasing again in high-income countries. This is in contrast with the card payment, for which the adoption rate increases monotonically in per capita income across countries. Also, advanced economies and developing countries tend

\textsuperscript{5}See a speech by Lael Brainard, a Federal Reserve governor, on “Delivering Fast Payments for All” on August 5, 2019.
to adopt different mobile payment solutions: The former favor those complementary to card, while the latter favor those substituting card.

We then construct a theory to explain the early success of advanced economies in adopting card payment, and how their advantage in card payment later hinders their adoption of mobile payment. In our model, three payment technologies, cash, card, and mobile, arrive sequentially. Newer payment technologies lower the variable costs of conducting payment transactions, but they require a fixed cost to adopt. When card arrives after cash, high-income consumers find it more attractive to adopt because they spend more on purchases and, thus, can save more on the variable costs of payment transactions. This explains the high adoption rate of card payments in rich countries. However, when mobile arrives after card, the adoption incentives are different between existing card users and cash users. Since the fixed cost for adopting card is already paid, card users face a higher income threshold to adopt mobile payments than cash users. As a result, the pre-mobile-payment composition of cash users and card users in each country leads to a non-monotonic relationship between mobile payment adoption and per capita income across countries, particularly the leapfrogging of low-income countries in mobile payment adoption. Moreover, since both card and mobile payment adoption requires fixed costs, cash users would favor mobile payments as a card-substituting solution, rather than paying the fixed costs to adopt both card and mobile payments. This explains why most developing countries choose Mobile Money, the mobile payment method bypassing card services. Card users, on the other hand, would more likely consider mobile payments complementary to card, which is why most advanced economies use card-complementing mobile solutions such as Apple Pay.

Our model calibration matches cross-country adoption patterns of both card and mobile payments well. Based on the calibrated model, we conduct quantitative analyses on several welfare and policy issues. We find that lagging behind in mobile payment adoption does not necessarily mean that advanced economies fall behind in overall payment efficiency, even though they benefit less from the mobile payment innovation compared with developing countries. Moreover, in our model economy, falling behind in adopting mobile payment is an optimal choice for advanced economies, and we provide a quantitative assessment of welfare loss of subsidizing mobile payment adoption. That said, our
model also suggests that greater technological advances in mobile payment are needed for advanced economies to regain leading positions in the payment race, and governments may play positive roles in facilitating technological progress and market coordination.

It is worth noting that our model focuses on the role of income heterogeneity in driving the adoption of payment technologies. In doing so, we largely abstract from network externality considerations. This is an intentional modeling choice for a couple of reasons. First, our paper aims to explain the steady-state payment adoption patterns rather than characterizing transitional paths, so there is less need to elaborate on the feedback loops among agents. Second, our approach, in the spirit of Ockham’s razor (or “the principle of parsimony”), allows us to fit the cross-country data well with a parsimonious model, which also facilitates the counterfactual and welfare analysis. Finally, we specify conditions in Section 6.1 under which our model indeed incorporates two-sided market network effects between consumers and merchants in terms of their payment choices. This interpretation of the model allows us to discuss issues otherwise veiled in a one-sided market setting, such as multiple equilibria and social versus private costs in adopting payment innovations. We point out that our model may serve as a first-order approximation if some of the conditions in Section 6.1 do not hold and we leave a full-blown two-sided market model for future research.

Our paper contributes to several strands of literature. The first one is theories of the payments system. Following the pioneering work of Baxter (1983), a fast growing body of literature has been developed for studying market structure and pricing of retail payments system, especially card payments (e.g., Rochet and Tirole, 2002, 2003, 2011, Wright, 2003, 2012, and Shy and Wang, 2011, among others; see Rysman and Wright, 2014, for a literature review). However, most of those studies assume a static setting and ignore adoption decisions of payment methods. Among very few exceptions, Hayashi, Li, and Wang (2017) and Li, McAndrews, and Wang (2020) study payment system evolution in dynamic settings, but they do not consider sequential innovations and leapfrogging, which is the focus of this paper.

The second one is the empirical investigation of consumer payment choices. While there is an abundance of literature studying domestic payment patterns (e.g., Rysman, 2007, Klee, 2008, Wang and Wolman, 2016, and Koulayev et al., 2016 for the U.S.),
cross-country studies on retail payments adoption are rather scarce and usually focus on developed economies. Among the few examples, Humphrey et al. (1996) compare the use of cash and noncash payment instruments in fourteen developed countries. Martikainen et al. (2015) examine the convergence of the European retail payments market, and Bagnall et al. (2016) document consumer cash use for seven developed countries using payment diary surveys. Cross-country comparison of mobile payments, however, has not been studied in this branch of literature. We fill this gap by compiling a novel dataset to study cross-country adoption patterns of mobile versus card payments. Our dataset includes both developed and developing economies, which allows us to uncover and address the leapfrogging puzzle.

Our paper is also related to the literature that studies how electronic payments affect financial inclusion and social well-being using large micro datasets. For example, Jack and Suri (2014) find that M-PESA (a mobile payment service in Kenya) reduced transaction costs of remittances and facilitated the risk-sharing networks of households. Muralidharan, Niehaus, and Sukhtankar (2016) show that biometrically authenticated cards enabled faster, more predictable, and less corrupt payments process for beneficiaries of employment and pension programs in India. Our paper complements these works in the sense that we take a quantitative macro approach to study how cost savings brought by electronic payments affect payment efficiency and drive different adoption patterns across countries.

Finally, our paper contributes to the broad literature of technology diffusion. For a long time, researchers have been interested in the relationship between the adoption of new technologies and the heterogeneity of potential adopters (e.g., Griliches, 1957). While some argue that the observed adoption lags are evidence of information or coordination frictions, Manuelli and Seshadri (2014) among others have shown that the speed of adoption can be well explained by the moving equilibrium of frictionless models. Moreover, in the presence of sequential innovations, some firms could get stuck with old technologies due to their past investments in technology-specific learning (e.g., Parente, 1994, Jovanovic and Nyarko, 1996, and Klenow, 1998). Our paper extends this line of research to a new context where consumers make frictionless adoption decisions on sequential payment innovations. We show high-income consumers or countries could be overtaken by
low-income counterparts in adopting mobile payments due to their past investments in precedent card payment technologies. Taking the theory to data, our quantitative model matches a non-monotonic relationship between mobile payment adoption and per capita income across countries, which is a novel empirical finding to the existing literature (e.g., Comin and Hobijn, 2004).

The remainder of this paper is structured as follows. Section 2 provides the background of mobile payment and summarizes stylized facts from a novel dataset regarding cross-country adoption patterns. Section 3 introduces the model and solves the equilibrium outcome. Section 4 calibrates the model and provides counterfactual exercises to illustrate the implications of the model. Section 5 conducts welfare and policy analyses. Section 6 provides further discussions. Finally, Section 7 concludes.

2 Background and stylized facts

Following Crowe et al. (2010), we define a mobile payment to be a money payment made for a product or service through a mobile phone, whether or not the phone actually accesses the mobile network to make the payment. Mobile payment technology can also be used to send money from person to person.

The very first mobile payment transaction in the world can be traced back to 1997, when Coca-Cola in Helsinki came out with a beverage vending machine, where users could pay for the beverage with just an SMS message. Around the same time, the oil company Mobil, also came out with an RFID (Radio Frequency Identification) device called Speedpass that allowed its users to pay for fuel at gas stations. These two earliest examples of mobile payment services were both based on the SMS and the payments were made by a mobile account that was linked to the user’s device.

The mobile payment systems based on SMS soon evolved into the world’s first phone-based banking service launched by the Merita Bank of Finland in 1997. Later, the mobile payment technology progressed with more user applications, such as buying movie tickets, ordering pizza, and arranging travels. In 2007, Vodafone launched one of the largest mobile payment systems in the world. It was based on SMS/USSD text messaging technology
and offered various kinds of macro and micro payments. Vodafone launched this service in Kenya and Tanzania with the cooperation of the local telecom operators.

The year 2011 witnessed major technology firms like Google and Apple entering the field of mobile payment. Google became the first major company to come up with a digital mobile wallet solution, Google Wallet. The wallet used the NFC (Near Field Communication) technology and allowed the customers to make payments, redeem coupons, and earn loyalty points. In 2014, Apple launched its mobile payment service in the United States called Apple Pay compatible with iPhone 6, which allowed the users to simply tap their phone against a contactless payment card terminal at the point of sale, paying instantaneously. Before long, competitors to Apple, such as Google and Samsung, released their respective apps, Android Pay (later merged with Google Wallet and became Google Pay) and Samsung Pay, in the wake of Apple Pay’s success.

As a cutting-edge payment innovation, mobile brings many additional benefits comparing with precedent card technologies, lowering both fixed and variable costs of making payments. First, given that mobile phone has been widely adopted in most countries, the fixed investment for adopting mobile payment is small for consumers and merchants. Second, mobile payment is fast, convenient, and more secure. Apple Pay, for example, enables the users to pay without unlocking their phones and the Touch/Face ID of an iPhone adds extra security to authenticate a purchase. Apple Pay also encrypts payment information by a tokenization technology, and, thus, enhances privacy and reduces the odds of fraud (Gupta et al., 2015). Third, as the mobile payment technology becomes more widespread, markets develop a system of complementary goods and services that further enhance users’ benefits, such as financial planning, rewards programs, and price competition (Crowe et al. 2010).7

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6SMS (Short Message Service) and USSD (Unstructured Supplementary Service Data) are two methods used by telecom companies to allow users to send and receive text messages. With SMS, messages are sent to SMS centers, which store the message and then transmit the message to the recipient. In contrast, USSD makes a direct connection between text message senders and recipients, making it more responsive.

7Crowe et al. (2010) provides detailed discussions on the long-run benefits of mobile payments. For example, consumers could have their payments automatically logged in their financial planning software. Also, they could upload warranties and instructional videos at the time of purchase. Merchants could engage in sophisticated rewards programs, where consumers could access their status from their mobile device and receive alerts when they are close to rewards thresholds. Also, consumers could compare prices at nearby stores. If it is relatively easy to add new payment mechanisms to a mobile device and to switch among options, one should see new entry and innovation in this arena.
2.1 Alternative mobile payment technologies

While there are many mobile payment solutions, they fall into two basic categories: either bypassing or complementing the existing bank-related payment card systems. In this paper, we name them card-substituting and card-complementing mobile payments, respectively. The former is mainly used in developing countries like Kenya, and the latter is popular in advanced economies like the United States.

2.1.1 Card-substituting mobile payment

Card-substituting mobile payment is epitomized by Kenya’s M-PESA model. M-PESA is a mobile payment service launched by Safaricom and Vodafone in Kenya in 2007. M-PESA users can deposit money into an account in their phones and send balances to other users by SMS text messages. Hence, they can use a mobile phone to (i) deposit and withdraw money, (ii) pay for goods and services, and (iii) transfer money to other users. To deposit and withdraw money, M-PESA users rely on M-PESA agents (e.g., shops, gas stations, post offices). These agents in the M-PESA system are the analogs of the ATMs and bank branches in the banking system, allowing the M-PESA operation to bypass the banking system.

Following the success in Kenya, M-PESA was emulated in many other developing countries. This category of mobile payment methods is defined as the “Mobile Money” payment by the Global System for Mobile Communications Association (GSMA) that meets the following conditions: First, the payment method must include transferring money as well as making and receiving payments using a mobile phone. Second, the payment method must be available to the unbanked (e.g., people who do not have access to a formal account at a financial institution). Third, the payment method must offer a network of physical transactional points (that can include agents) widely accessible to users. Fourth, mobile-banking-related payment services (such as Apple Pay and Google Wallet) that offer the mobile phone as just another channel to access a traditional banking product do not satisfy this definition of Mobile Money.

The global adoption of Mobile Money payment in 2018 is illustrated in Figure 2.\textsuperscript{8} The

percentage numbers in the figure refer to the shares of registered mobile money customers. The gray areas in the figure represent regions where the Mobile Money payment services are unavailable. Most users of Mobile Money payment are concentrating in developing countries, particularly sub-Saharan Africa (45.6%) and South Asia (33.2%). In contrast, Mobile Money payment services are barely relevant for developed countries.

Figure 2. Global Adoption of Mobile Money Payment

2.1.2 Card-complementing mobile payment

Card-complementing mobile payment is typically deployed in developed countries. The popular types, created by technology firms (e.g., Apple, Google, Samsung), rely heavily on banking and payment card networks. Because of using a proximity communication technology (e.g., NFC or QR codes), these payment types are often referred to as mobile proximity payment services.

Apple Pay is a leading example. Apple Pay was launched in 2014 as one of the first mobile wallets — apps that enable people to connect credit cards, debit cards, and bank accounts to mobile devices to send and receive money. Of the major mobile wallet services — Google Pay (formerly Android Pay), Samsung Pay and Apple Pay — the Apple service is the largest in terms of user adoption and market coverage.

Apple Pay represents a secure and sanitary payment option, since the app uses the NFC technology to transmit an encrypted virtual account number to the point-of-sale payment terminal. Originally launched in the United States, Apple Pay debuted in the
United Kingdom, Australia, and Canada in 2015, and expanded to China, Switzerland, France, Singapore, and Japan in 2016. By 2020, Apple Pay has become available in dozens of countries (marked dark blue in Figure 3), most of which are developed countries.\(^9\) Apple Pay supports both international payment card networks—such as American Express, Visa, Mastercard, and Discover—as well as country-specific domestic payment card services like China’s UnionPay, Japan’s JCB, France’s Cartes Bancaires, and Canada’s Interac.

Figure 3. Global Availability of Apple Pay

2.2 Data and stylized facts

To study the global adoption pattern of mobile payments, we assembled a novel dataset on debit card and mobile payment adoption in 94 countries.\(^{10}\) The countries in our sample accounted for 91.4% of world GDP in 2017.

The dataset are drawn from the following sources (See Appendix I for more details). First, the data on the adoption rate of card-substituting mobile payment services in 2017 are based on the Global Financial Inclusion (Global Findex) Database of the World Bank, which surveyed 76 countries with a visible presence of Mobile Money payment services. Second, the data on the adoption rate of card-complementing mobile payments

\(^9\)Source: https://en.wikipedia.org/wiki/Apple_Pay#Supported_countries.
\(^{10}\)Debit card ownership is a good measure of consumers who have access to card-payment technologies because credit card users almost surely own debit cards. For robustness checks, we also redid the analysis using an alternative measure from the World Bank dataset on the percentage of the adult population (age 15 and above) using a debit or credit card to make a purchase in the past year. The results are very similar.
around 2017, gathered from eMarketer, cover 23 countries with a visible presence of mobile proximity payment services. Merging the two mobile payment data sources yields a sample of 94 countries, among which five countries are covered in both data sources. We also collect the adoption rate of debit cards for the 94 countries in 2017 from the Global Findex Database of the World Bank. Finally, we obtain the data on per capita GDP for each country in our sample from the World Bank.

Figure 4 plots the adoption rates of debit card and mobile payments against log per capita GDP in 2017. Fitting a simple linear regression line to the data shows that debit card adoption rate strictly increases in per capita GDP across countries, while there appears no clear relationship between mobile payment adoption and per capita GDP.

However, as we delve further into the mobile payment adoption data, some pattern starts to emerge. First, we divide the sample into three income groups: low-income countries (i.e., per capita GDP < $2,500), middle-income countries (i.e., $2,500 ≤ per capita GDP ≤ $30,000), and high-income countries (i.e., per capita GDP > $30,000). We then distinguish different payment technologies used in each country in the sample. As shown in Figure 5A, there are clear differences in mobile payment technology choice: Most low- and middle-income countries choose card-substituting mobile payment, while most high-income countries choose card-complementing mobile payment.
Considering that mobile payment is a fairly recent technological innovation, it is possible that some countries (including those not covered by our dataset) may not have fully introduced it due to information or coordination frictions. We then remove the observations that have very low adoption rate (i.e., <10%) and add back linear regression lines by income-country group. The results are shown in Figure 5B. It becomes visible that mobile payment adoption displays a non-monotonic relationship with per capita GDP: increasing in low-income countries, decreasing in middle-income countries, and increasing again in high-income countries. We report the regression results in Appendix II, and these patterns are robust for using a nonlinear regression model or an instrumental variable approach.

![Figure 5. Cross-Country Mobile Payment Adoption Pattern](image)

To sum up, we have documented the following stylized facts on cross-country adoption patterns of card and mobile payments:

1. **Positive relation between per capita income and card adoption.** – The adoption of card increases in per capita income across countries.

2. **Non-monotonic relation between per capita income and mobile payment adoption.** –

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Removal of observations with mobile payment adoption rates below 10% only affects countries from the Global Findex Database that use Mobile Money payment services. Presumably, the eMarketer dataset on mobile proximity payment adoption has implicitly applied a similar selection rule.
The adoption of mobile payment increases in per capita income in low- and high-income countries, but decreases in per capita income in middle-income countries.

3. Overtaking in mobile payment adoption. – Some low-income countries overtake high-income countries in adopting mobile payment.

4. Different technology choices across countries. – Low- and middle-income countries primarily adopt the card-substituting mobile payment technologies, while in high-income countries, the dominant choices are the card-complementing ones.

In the rest of the paper, we will construct a theory to explain these stylized facts and conduct welfare and policy analyses. We will also provide discussions on the outlier countries with very low mobile payment adoption rates (i.e., <10%) in Section 6.

3 Model

In this section, we provide a model with sequential payment innovations to explain the stylized facts documented above. We outline the model environment in Section 3.1 and then characterize the model equilibrium in Section 3.2.

3.1 Setup

Our model studies the adoption of payment technologies across countries. In each country, three payment technologies arrive sequentially, in the order of cash, card, and mobile.

Cash is a traditional paper payment technology, accessible to everyone in an economy. Using cash incurs a cost \( \tau_h \) per dollar of transaction, which includes handling, safekeeping, and fraud expenses. In contrast, card and mobile are electronic payment technologies, each of which requires a fixed cost of adoption but lowers variable costs of doing transactions comparing with cash.\(^{12}\) We denote \( k_d \) and \( k_m \) as the one-time fixed adoption costs associated with card and mobile, respectively. Those fixed costs may include resources spent on joining banking or mobile payment networks plus the costs of acquiring the hardware and software for making electronic payments. The variable costs associated with

\(^{12}\)A main reason for electronic payments to be used, despite of the fixed adoption costs, is that they reduce the variable costs of payments (e.g., the time of dealing with handling, safekeeping, and fraud).
with using card and mobile are denoted as \( \tau_d \) and \( \tau_m \) per dollar of transaction, respectively. To capture the technology progress between cash, card, and mobile, we assume \( \tau_h > \tau_d > \tau_m \) and \( k_d > k_m \).

Time is discrete with an infinite horizon. We consider an economy where agents' incomes are exogenous and heterogeneous (e.g., due to differences in productivity). Without loss of generality, we assume that income \( I_t \) at time \( t \) follows an exponential distribution across the population in the economy, with the cumulative distribution function (cdf) \( G_t(I_t) = 1 - \exp(-I_t/\lambda_t) \).\(^{13}\) Note that the exponential distribution has a fixed Gini coefficient at 0.5 and the mean is \( \lambda_t \). Over time, each agent's income grows at a constant rate \( g \), i.e., \( I_{t+1} = I_t(1 + g) \), as does the mean income of the economy, i.e., \( \lambda_{t+1} = \lambda_t(1 + g) \). We normalize the population size to unity.

An agent has a linear utility \( u = c \), where \( c \) is her consumption. We assume no storage technology, so each agent consumes all her income net of payment costs each period. We also assume payment services and merchant services are provided by competitive markets so that a consumer can always use her favorite payment technology at its social cost.\(^{14}\)

### 3.2 Equilibrium

We derive the equilibrium adoption patterns of cash, card, and mobile payment technologies as they arrive sequentially in an economy.

#### 3.2.1 Cash payment

Cash is the only payment technology available in the economy before electronic payments are introduced. Cash is accessible to everyone, so the adoption rate is 100%. In such a cash economy, the value function \( V_h \) of an agent depends on her income \( I_t \), and can be written as

\[
V_h(I_t) = (1 - \tau_h)I_t + \beta V_h(I_{t+1}),
\]

where \( I_{t+1} = I_t(1 + g) \).

\(^{13}\)The exponential distribution fits income distributions well (e.g., see Dragulescu and Yakovenko, 2001).

\(^{14}\)These simplifying assumptions allow us to focus on the technological side of payment innovations and provide a good benchmark for understanding the key cross-country differences. We provide more discussions in Section 6 on these assumptions.
and $\beta$ is the discount rate. Accordingly, $V_h(I_{t+1}) = (1 + g)V_h(I_t)$, and we derive

$$V_h(I_t) = \frac{(1 - \tau_h) I_t}{1 - \beta(1 + g)}.$$  \hfill (1)

### 3.2.2 Card payment

At time $T_d$, the payment card technology arrives as an exogenous shock. Each agent then compares card and cash technologies and makes the adoption decision.

At any point of time $t \geq T_d$, the value function $V_d$ of an agent who has income $I_t$ and has adopted card can be written as

$$V_d(I_t) = (1 - \tau_d)I_t + \beta V_d(I_{t+1}),$$

which yields

$$V_d(I_t) = \frac{(1 - \tau_d) I_t}{1 - \beta(1 + g)}.$$  \hfill (2)

The availability of the card technology also changes the value function of cash users because it adds an option of adopting card in the future. Therefore, the value function of an agent who has income $I_t$ and decides to continue using cash at time $t$ would be

$$V_h(I_t) = (1 - \tau_h)I_t + \beta \max\{V_h(I_{t+1}), V_d(I_{t+1}) - k_d\}.$$  \hfill (3)

At each point of time $t \geq T_d$, an agent would adopt card if and only if

$$V_d(I_t) - k_d \geq V_h(I_t).$$  \hfill (4)

Therefore, Eqs. (2), (3), and (4) pin down the minimum income level $I_d$ for card adoption, which requires

$$\frac{(1 - \tau_d) I_d}{1 - \beta(1 + g)} - k_d = (1 - \tau_h)I_d + \beta\left[\frac{(1 - \tau_d)(1 + g)I_d}{1 - \beta(1 + g)} - k_d\right].$$

Accordingly, an agent would have adopted card by time $t \geq T_d$ if and only if her income satisfies that

$$I_t \geq I_d = \frac{(1 - \beta)k_d}{\tau_h - \tau_d}.$$  \hfill (5)
The intuition of condition (5) is straightforward: An agent would adopt card if the flow benefit of adoption \((τ_h - τ_d)I_t\) can cover the flow cost \((1 - β)k_d\).

The payment card adoption rate, \(F_{d,t}\), is determined as

\[
F_{d,t} = 1 - G_t(I_d) = \exp\left(-\frac{(1 - β)k_d}{(τ_h - τ_d)λ_t}\right). \tag{6}
\]

It follows immediately from Eq. (6) that the payment card adoption rate increases in per capita income (i.e., \(∂F_{d,t}/∂λ_t > 0\)).

3.2.3 Mobile payment

Mobile payment arrives after card as another exogenous shock. In the following, we first study a scenario where only a card-substituting mobile payment technology (e.g., Mobile Money) is introduced, and we then study another scenario where a card-complementing mobile payment technology, (e.g., Apple Pay) also becomes available.

A card-substituting mobile payment technology

At a point of time \(T_m > T_d\), a card-substituting mobile payment technology arrives. This mobile payment technology allows users to replace or bypass the card technology, with a lower marginal cost \(τ_m < τ_d < τ_h\) and a lower fixed cost \(k_m < k_d\). Each agent then compares three payment technologies (i.e., cash, card, and mobile) to make the adoption decision.

At any point \(t ≥ T_m\), the value function \(V_m\) of an agent who has income \(I_t\) and has adopted mobile can be written as

\[
V_m(I_t) = (1 - τ_m)I_t + βV_m(I_{t+1}),
\]

which yields

\[
V_m(I_t) = \frac{(1 - τ_m)I_t}{1 - β(1 + g)}. \tag{7}
\]

Because mobile is a better payment technology than card, (i.e., \(τ_m < τ_d\) and \(k_m < k_d\)), an agent who has not adopted card by time \(T_m - 1\) (i.e., \(I_{T_m-1} < I_d\)) would no longer consider adopting card at time \(T_m\) and afterwards. Instead, they would adopt mobile payment at a point of time \(t ≥ T_m\) whenever
\[
V_m(I_t) - k_m \geq V_h(I_t),
\]  
(8)

where the value function of a cash user \(V_h(I_t)\) now becomes

\[
V_h(I_t) = (1 - \tau_h)I_t + \beta \max\{V_h(I_{t+1}), V_m(I_{t+1}) - k_m\}.
\]  
(9)

Equations (7), (8), and (9) then pin down the minimum income level \(I_m\) for mobile payment adoption:

\[
I_t \geq I_m = \frac{(1 - \beta)k_m}{(\tau_h - \tau_m)}.
\]  
(10)

Given \(\tau_m < \tau_d < \tau_h\) and \(k_m < k_d\), Eqs. (5) and (10) show \(I_m < I_d\), so the fraction of agents who have switched from cash to mobile by time \(t \geq T_m\) is

\[
F_{h\rightarrow m,t} = G_{T_m-1}(I_d) - G_t(I_m) = \exp(-I_m/\lambda_t) - \exp(-I_d/\lambda_{T_m-1}) \]  
(11)

\[
\quad = \exp\left(-\frac{(1 - \beta)k_m}{(\tau_h - \tau_m)\lambda_t}\right) - \exp\left(-\frac{(1 - \beta)k_d}{(\tau_h - \tau_d)\lambda_{T_m-1}}\right).
\]

Equations (7), (12), and (13) pin down the income level \(I_{m'}\) above which agents would switch from card to mobile payment:

\[
V_m(I_t) - k_m \geq V_c(I_t),
\]  
(12)

where the value function of a card user now becomes

\[
V_c(I_t) = (1 - \tau_d)I_t + \beta \max\{V_c(I_{t+1}), V_m(I_{t+1}) - k_m\}.
\]  
(13)

Equations (7), (12), and (13) pin down the income level \(I_{m'}\) above which agents would switch from card to mobile payment:

\[
I_t \geq I_{m'} = \frac{(1 - \beta)k_m}{(\tau_d - \tau_m)}.
\]  
(14)

Equations (5) and (14) suggest that as long as \(\frac{k_m}{\tau_d - \tau_m} > \frac{k_d}{\tau_h - \tau_d}\), we have \(I_{m'} > I_d\).\(^{15}\) So

\(^{15}\)The condition \(\frac{k_m}{\tau_d - \tau_m} > \frac{k_d}{\tau_h - \tau_d}\) ensures that \(I_{m'} > I_d\), so only a fraction of the consumers who have
the fraction of agents who have switched from card to mobile by time $t \geq T_m$ is

$$F_{d-m,t} = 1 - G_t(I_m') = \exp(-I_m'/\lambda_t)$$

as long as some card adopters have not adopted mobile (i.e., $F_{d-m,t} < F_{d,T_m-1}$). Otherwise, $F_{d-m,t} = F_{d,T_m-1}$.

Combining Eqs. (11) and (15), the total fraction of agents who have adopted mobile payments by time $t \geq T_m$ is

$$F_{m,t} = F_{h-m,t} + F_{d-m,t} = \exp(-I_m/\lambda_t) - \exp(-I_d/\lambda_{T_m-1}) + \exp(-I_m'/\lambda_t)$$

as long as $F_{d-m,t} < F_{d,T_m-1}$. Otherwise, $F_{m,t} = \exp(-I_m/\lambda_t) = \exp(-\frac{(1-\beta)k_m}{(\tau_h - \tau_m)\lambda_t})$. This result unveils the following subtle relationship between the mobile payment adoption rate and per capita income: (i) taking the value of $\lambda_{T_m-1}$ as given, Eq. (16) yields $\partial F_{m,t}/\lambda_t > 0$, which implies that a country’s mobile payment adoption rate increases over time due to income growth; (ii) taking into account $\lambda_{T_m-1} = \lambda_t/(1 + g)^{t-T_m+1}$, Eq. (16) shows that the sign of $\partial F_{m,t}/\lambda_t$ has to depend on parameter values. As a result, the mobile payment adoption rate may not show a monotonic relationship with per capita income across countries; and (iii) in the long run, once all the card adopters eventually adopt mobile (i.e., $F_{d-m,t} = F_{d,T_m-1}$), we have $F_{m,t} = \exp(-I_m/\lambda_t) = \exp(-\frac{(1-\beta)k_m}{(\tau_h - \tau_m)\lambda_t})$, in which case the mobile payment adoption rate becomes strictly increasing in per capita income across countries (i.e., $\partial F_{m,t}/\partial \lambda_t > 0$).

**A card-complementing mobile payment technology** We now extend the model to consider another scenario that at the same point of time $T_m$, a card-complementing mobile payment solution also becomes available in addition to the card-substituting one.
This mobile payment technology is an add-on upgrade to the existing card technology, which allows an agent who has adopted card to pay an upgrading cost \( k_m^a \) to get the mobile payment feature that lowers the variable cost of payments (i.e., \( \tau_h > \tau_d > \tau_m \)). This add-on technology requires a lower fixed cost than adopting the card-substituting mobile payment method (i.e., \( k_m^a < k_m \)).

It is straightforward to see that in this scenario, agents who have adopted card before \( T_m \) would prefer adopting the card-complementing mobile payment technology because \( k_m^a < k_m \), while agents who have not adopted card would bypass card and adopt the card-substituting mobile payment technology because \( k_m < k_d + k_m^a \).

Therefore, agents who have switched from cash to mobile by time \( t \geq T_m \) should have chosen the card-substituting mobile payment technology. As shown in Eq. (11) above, the fraction of these agents is

\[
F_{h \rightarrow m, t} = G_{T_m - 1}(I_d) - G_t(I_m) = \exp\left(-\frac{(1 - \beta)k_m}{(\tau_h - \tau_m)\lambda_t}\right) - \exp\left(-\frac{(1 - \beta)k_d}{(\tau_h - \tau_d)\lambda_{T_m - 1}}\right).
\]

On the other hand, agents who have chosen the card-complementing mobile payment by time \( t \geq T_m \) are those whose income have crossed the threshold

\[
I_t \geq I_m^a = \frac{(1 - \beta)k_m^a}{(\tau_d - \tau_m)}.
\]  

The fraction of these card-mobile switchers is

\[
F_{d \rightarrow m, t} = 1 - G_t(I_m^a) = \exp\left(-\frac{(1 - \beta)k_m^a}{(\tau_d - \tau_m)\lambda_t}\right),
\]  

as long as \( F_{d \rightarrow m, t} \leq F_{d, T_m - 1} \), a result similar to what is derived in Eq. (15) except that \( k_m^a \) replaces \( k_m \). Otherwise, \( F_{d \rightarrow m, t} = F_{d, T_m - 1} \).

All together, the total fraction of agents who have adopted mobile payments by time \( t \geq T_m \) is

\[
F_{m, t} = F_{h \rightarrow m, t} + F_{d \rightarrow m, t} = \exp\left(-\frac{(1 - \beta)k_m}{(\tau_h - \tau_m)\lambda_t}\right) - \exp\left(-\frac{(1 - \beta)k_d}{(\tau_h - \tau_d)\lambda_{T_m - 1}}\right) + \exp\left(-\frac{(1 - \beta)k_m^a}{(\tau_d - \tau_m)\lambda_t}\right).
\]
as long as \( F_{d \to m, t} < F_{d, T_m - 1} \). Otherwise, \( F_{m, t} = \exp(-\frac{I_m}{\lambda_t}) = \exp(-\frac{(1-\beta)k_m}{(\tau_h - \tau_m)\lambda_t}) \).

Again, Eq. (19) implies that depending on parameter values, the mobile payment adoption rate \( F_{m, t} \) may not have a monotonic relationship with per capita income \( \lambda_t \) across countries. But once all the card adopters have adopted mobile so that \( F_{m, t} = \exp(-\frac{I_m}{\lambda_t}) = \exp(-\frac{(1-\beta)k_m}{(\tau_h - \tau_m)\lambda_t}) \), the mobile payment adoption rate becomes strictly increasing in per capita income across countries.

4 Model calibration and implications

In this section, we calibrate the model to match the cross-country card and mobile payment adoption patterns. We then conduct counterfactual analyses to explore the model implications regarding different mobile payment options, income growth, and technological progress.

4.1 Model calibration

We first calibrate the model with two mobile payment options (i.e., the card-substituting and card-complementing ones) using the parameter values as shown in Table 1.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Description</th>
<th>Source of Identification</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \beta )</td>
<td>0.95</td>
<td>Discount factor</td>
<td>Standard</td>
</tr>
<tr>
<td>( g )</td>
<td>2%</td>
<td>Income growth rate</td>
<td>Standard</td>
</tr>
<tr>
<td>( \tau_h )</td>
<td>2.3%</td>
<td>Cash variable cost</td>
<td>Schmiedel et al. (2012)</td>
</tr>
<tr>
<td>( \tau_d )</td>
<td>1.4%</td>
<td>Card variable cost</td>
<td>Schmiedel et al. (2012)</td>
</tr>
<tr>
<td>( k_d )</td>
<td>500</td>
<td>Card adoption cost</td>
<td>Cross-country card payment adoption pattern, Figure 6A</td>
</tr>
<tr>
<td>( \tau_m )</td>
<td>1.395%</td>
<td>Mobile variable cost</td>
<td>Cross-country mobile payment adoption pattern, Figure 6B</td>
</tr>
<tr>
<td>( k_m )</td>
<td>150</td>
<td>Mobile adoption cost</td>
<td>Cross-country mobile payment adoption pattern, Figure 6B</td>
</tr>
<tr>
<td>( k_{m0} )</td>
<td>100</td>
<td>Mobile add-on cost</td>
<td>Cross-country mobile payment adoption pattern, Figure 6B</td>
</tr>
</tbody>
</table>

The unit of time is year, and we set 2017 as the year \( T_m \) when mobile payment becomes available. Following convention, we set the discount factor \( \beta = 0.95 \) and the
annual income growth rate $g = 2\%$. According to an ECB study (Schmiedel et al., 2012) on retail payment costs in 13 participating countries, the average social cost of using cash is 2.3% of the transaction value, while that of using debit cards is 1.4%, so we set the values of $\tau_h$ and $\tau_d$ accordingly. We then calibrate $k_d = 500$ to fit the cross-country card adoption pattern in 2017. Finally, we calibrate the mobile payment variable cost $\tau_m = 1.395\% (< \tau_d)$ and the fixed costs $k_m = 150 (< k_d)$ and $k_m^a = 100 (< k_m)$ to fit the cross-country mobile payment adoption pattern in 2017.\textsuperscript{16,17}

![Figure 6. Model Fit with Data](image)

Figure 6 shows that our calibration results fit the data well and match the first three stylized facts identified above: (1) Positive relation between per capita income and card adoption; (2) Non-monotonic relation between per capita income and mobile payment adoption; (3) Overtaking in mobile payment adoption.

\textsuperscript{16}To discipline the calibration, we assume that all countries share the same model parameter values and the card-substituting and card-complementing mobile payment technologies share the same value of $\tau_m$. Relaxing such assumptions would provide additional degrees of freedom and, thus, allow the model to fit the data targets even better.

\textsuperscript{17}In the model calibration, we treat per capita income/spending and per capita GDP interchangeable. In reality, per capita income/spending could be a fraction of per capita GDP. To account for that, we can simply rescale the payment adoption costs (i.e., $k_d$, $k_m$, and $k_m^a$) by the same fraction without affecting our analysis and findings. Similarly, note that the equilibrium adoption rates in our model all depend on the ratios (i.e., $\frac{k_d}{\tau_d - \tau_m}$, $\frac{k_m}{\tau_d - \tau_m}$, $\frac{k_m^a}{\tau_d - \tau_m}$, and $\frac{k_m}{\tau_d - \tau_m}$). In case that the calibrated values of $\tau_h$, $\tau_d$ and $\tau_m$ that we use are mismeasured by a certain fraction, we can also rescale the payment adoption costs (i.e., $k_d$, $k_m$, and $k_m^a$) accordingly.
Figure 7 below shows that our calibration also matches the fourth stylized fact: (4) 

*Different technology choice across countries.* In Figure 7, we decompose the fraction of total mobile payment adopters at $T_m = 2017$ (red dash line) into cash-mobile switchers (green solid line) and card-mobile switchers (blue solid line) by per capita income, and compare with the fractions of previous cash users (green dot line) and card users (blue dot line) at $T_m - 1$. In the low-income countries (i.e., $\lambda_{T_m} < 2,500$) and most middle-income countries (i.e., $2,500 \leq \lambda_{T_m} \leq 30,000$), mobile payment adoption almost entirely relies on cash-mobile switchers who choose card-substituting technologies, while in most high-income countries (i.e., $\lambda_{T_m} > 30,000$), mobile payment adoption relies on card-mobile switchers who choose card-complementing technologies.

Moreover, Figure 7 helps explain the non-monotonic relation between per capita income and mobile payment adoption. In the low-income countries, because most agents are cash users, the adoption of mobile payments concentrates on card-substituting technologies and the adoption increases in per capita income. By contrast, in the middle-income countries, because more agents are card users who are locked in by the card technology (i.e., their income cannot justify switching to either card-substituting or card-complementing mobile payment technologies), the adoption of mobile payment decreases in per capita income. Finally, in the high-income countries, most agents are card users.
and their incomes are high enough to justify switching to the card-complementing mobile payment technology, so the adoption of mobile payment again increases in per capita income.

4.2 Model implications

Our calibrated model matches the average cross-country pattern of mobile payment adoption. Based on the model, we provide several counterfactual exercises to illustrate the implications of the model.

4.2.1 Mobile payment options

We first check how the availability of different mobile payment technology options affect the adoption pattern, as shown in Figure 8 below. The green dash line shows the mobile payment adoption pattern if only the card-substituting option is available in each country. The blue dot line shows the adoption pattern if only the card-complementing option is available in each country. The red solid line, as seen above, shows the adoption pattern when both mobile payment options are available in each country.

![Figure 8. Mobile Payment Options and Adoption Patterns](image)

The results in Figure 8 provide the following insights on the effects of mobile payment technology options:
First, the availability of both mobile payment options in each country increases adoption rate, especially for high-income countries. As shown in the figure, the red line is on top of both the green dash line and the blue dash line.

Second, only having the card-substituting mobile payment option in each country would not change much of the cross-country adoption pattern. Its effects on low- and middle-income countries are almost entirely negligible, though it pushes down mobile payment adoption in high-income countries almost by half.

Third, only having the card-complementing mobile payment option, however, would overturn the cross-country adoption pattern, making adoption increasing in per capita income. Essentially, it would kill mobile payment adoption in most low- and middle-income countries, and it pushes down only slightly mobile payment adoption in high-income countries.

Finally, with both mobile payment technologies being available, it is possible that each country, depending on its per capita income, may only choose to supply one type of mobile payment technology (e.g., due to network effects or a minimum scale requirement). If that is the case, the adoption pattern would be given by the upper envelope of the green dash line and the blue dot line. In this case, the cross-country adoption pattern does not change much comparing with our calibrated model.\(^{18}\)

### 4.2.2 Income growth

We now consider the effect of income growth. According to our theory, long-run income growth would eventually take all the card adopters who exist before time \(T_m\) to cross the mobile payment adoption threshold. Once that happens, the mobile payment adoption would solely depend on cash-mobile switchers, and the adoption rate would become increasing monotonically in per capita income. However, our quantitative exercise suggests that it would just take too long for income growth to overturn the non-monotonic mobile payment adoption pattern.

Recall that we assume per capita income grows at 2% annually in each country. Figure

\(^{18}\)An alternative way to calibrate our model is to assume that a country only supplies one type of mobile payment technology, either the card-substituting one or the card-complementing one, whichever would yield the higher adoption rate. However, Figure 8 suggests that this alternative calibration would not change much of the data fitting, and the counterfactual analyses would be very similar.
9 tracks each country by per capita income at time $T_m$ and plots mobile payment adoption rates at year $T_m$ (red solid line), $T_m + 50$ (pink dash line), $T_m + 100$ (green dot line), and $T_m + 180$ (blue dash-dot line). It shows that as per capita income grows, mobile payment adoption increases in every country. Meanwhile, the adoption rate continues to be non-monotonic in per capita income. Ultimately, it takes 180 years to converge to an adoption curve that strictly increases in per capita income.\textsuperscript{19}

![Figure 9. Income Growth and Mobile Payment Adoption](image)

Figure 9 decomposes mobile payment adopters into cash-mobile switchers and card-mobile switchers. It shows that as per capita income grows over time, both cash-mobile switchers and card-mobile switchers increase in every country. Eventually, once all the previous card users have adopted mobile payment at year $T_m + 180$ in every country, the remaining adoption is determined solely by cash-mobile switchers and the overall mobile payment adoption rate strictly increases in per capita income.

\textsuperscript{19}In our model simulation, with the 2\% annual income growth rate, all the agents who have adopted card by $T_m - 1$ would have crossed the mobile payment adoption threshold in 180 years. Once that happens, the mobile payment adoption rate is simply the fraction of agents whose incomes are greater than $I_m$ (i.e., the income threshold for cash-mobile switchers), and it increases in per capita income $\lambda_I$. Note that this process could speed up if our model introduces birth and death of agents.
Figure 10. Income Growth and Mobile Payment Adopters

4.2.3 Technological progress

Comparing with income growth, the effect of technological progress on mobile payment adoption can be more striking. According to our theory, the main reason that advanced economies are stuck with card payment is because the value added of mobile payment is not substantial enough. Therefore, greater technological progress of mobile payment not only would increase the adoption in every country, but also could restore advanced economies to the leading positions in the mobile payment race if the technological progression is sufficiently large.

To see this, we conduct a counterfactual exercise with different values of $\tau_m$. The results are plotted in Figure 11. It shows that with larger technological progress (i.e., smaller values of $\tau_m$), the mobile payment adoption rate gets higher in every country and advanced economies are especially benefitted. If the technological progress is sufficiently large, mobile payment adoption becomes strictly increasing in per capita income across countries.
Taking a step further, Figure 12 decomposes mobile payment adopters into cash-mobile switchers and card-mobile switchers. One can see technological progress mainly boosts mobile payment adoption among previous card users who enjoy more cost savings than cash users through a lower $\tau_m$ due to their higher income and spending. This explains why high-income countries benefit more. Therefore, should some major technological progress occur down the road, advanced economies might see their mobile payment adoption jump up and they may even regain leading positions in the mobile payment race.
5 Welfare and policy analyses

In this section, we use our calibrated model to conduct welfare and policy analyses.

5.1 Payment efficiency

Given our model framework, an intriguing question is to identify the winners and losers in adopting new payment technologies. To address this question, we conduct a welfare analysis. We first evaluate payment efficiency for individual agents and then for aggregate economies. For ease of notation, we denote each agent by her income level $I$ (without the time subscript) in the analysis.

5.1.1 Individual agents

We first consider individual agents in a cash economy. Denote $V_h(I)$ as the value function of an agent $I$ who would permanently use cash payment. By Eq. (1), we know

$$V_h(I) = \frac{(1 - \tau_h) I}{1 - \beta (1 + g)}, \quad (20)$$

so the present-value welfare of agent $I$, denoted by $\bar{\omega}_t(I)$, equals $V_h(I)$ for any $t < T_d$.

At time $T_d$, the card technology arrives as an exogenous shock. Denote $V_d(I)$ as the value function of an agent $I$ who would permanently use card payment. By Eq. (2), we know

$$V_d(I) = \frac{(1 - \tau_d) I}{1 - \beta (1 + g)}, \quad (21)$$

The present-value welfare of agent $I$ at time $T_d$, denoted by $\omega_{T_d}(I)$, depends on the agent’s income and the corresponding card adoption:

$$\omega_{T_d}(I) = \begin{cases} 
V_d(I) - k_d & \text{if } I \geq I_d; \\
V_h(I) + \beta^s \left[ V_d(I(1 + g)^s) - k_d - V_h(I(1 + g)^s) \right] & \text{if } \frac{I_d}{(1+g)^s} \leq I < \frac{I_d}{(1+g)^{s-1}}, \quad (22)
\end{cases}$$

for $s \in \{1, 2, 3, \ldots\}$. Note that $I_d = \frac{(1-\beta)k_d}{(\tau_h - \tau_d)}$ is given by Eq. (5). The top equation of (22) calculates the welfare of an agent whose income crosses the card adoption threshold at time $T_d$, and the bottom
equation calculates the welfare of an agent who would adopt card at a future time.

At time $T_m$, the mobile payment arrives. Denote $V_m(I)$ as the value function of an agent $I$ who would permanently use mobile payment. By Eq. (7), we know

$$V_m(I) = \frac{(1 - \tau_m) I}{1 - \beta(1 + g)}.$$  \hfill (23)

The present-value welfare of agent $I$ at time $T_m$, denoted by $\omega_{T_m}(I)$, depends on the agent’s income and the corresponding mobile payment adoption:

$$\omega_{T_m}(I) = \begin{cases} 
    \bar{V}_m(I) - k_m^a 
    & \text{if } I \geq I_m^a; \\
    \tilde{V}_d(I) + \beta^a \begin{bmatrix} 
        \tilde{V}_m(I(1 + g)^s) \\
        -k_m^a - \tilde{V}_d(I(1 + g)^s)
    \end{bmatrix} 
    & \text{if } \max(I_m, I_d(1 + g)) \leq I < \frac{I_m^a}{(1 + g)^{s - 1}}, \\
    \bar{V}_m(I) - k_m 
    & \text{if } I_m \leq I < I_d(1 + g); \\
    \bar{V}_h(I) + \beta^s \begin{bmatrix} 
        \tilde{V}_m(I(1 + g)^s) \\
        -k_m - \bar{V}_h(I(1 + g)^s)
    \end{bmatrix} 
    & \text{if } \frac{I_m}{(1 + g)^{s - 1}} \leq I < \frac{I_m}{(1 + g)^{s}}, \\
    \bar{V}_m(I) - k_m^a 
    & \text{for } s \in \{1, 2, 3, \ldots\}; \\
    \bar{V}_h(I) + \beta^a \begin{bmatrix} 
        \tilde{V}_m(I(1 + g)^a) \\
        -k_m - \bar{V}_h(I(1 + g)^a)
    \end{bmatrix} 
    & \text{for } s \in \{1, 2, 3, \ldots\}. 
\end{cases}$$  \hfill (24)

Note that $I_m = \frac{1 - \beta k_m}{\tau_h - \tau_m}$ is given by Eq. (10), and $I_m^a = \frac{1 - \beta k_m^a}{\tau_d - \tau_m}$ is given by Eq. (17). The top equation of (24) calculates the welfare of a card-mobile switcher whose income crosses the mobile adoption threshold at time $T_m$, and the second equation is the welfare of a card user who would adopt mobile at a future time. The third equation is the welfare of a cash-mobile switcher at time $T_m$, and the bottom equation is the welfare of a cash user who would adopt mobile at a future time.

Define the payment efficiency of an agent $I$, $x_t(I)$, as the ratio between the present value of welfare at time $t$ with and without incurring the payment costs:

$$x_t(I) = \frac{\omega_t(I)}{1 - \beta(1 + g)}.$$  \hfill (25)

Note that the denominator, $1 - \beta(1 + g)$, is the first-best welfare in a frictionless economy without any payment costs, so $x_t(I)$ gauges the fraction of the first-best welfare level that can be achieved by agent $I$ under available payment technologies at time $t$.

Using the parameter values in Table 1, we can compare payment efficiency for individual agents at different income levels under each payment innovation. As before, we
assume that the mobile payment technology arrives at $T_m = 2017$. We then assume that the card payment arrives at $T_d = T_m - 30$. Figure 13 plots the payment efficiency of each agent for $t < T_d$ (i.e., cash only), $t = T_d$ (i.e., card becomes available), $t = T_m$ (i.e., mobile becomes available), according to their individual income level at $T_m$. For a comparison, we also plot a counterfactual case for $t = T_m$ assuming mobile does not become available then, which we denoted as $\tilde{x}_{T_m}$.

Figure 13 shows that every agent has the same payment efficiency when cash is the only payment means (i.e., $x_t < T_d = 1 - \tau_h$). Once the card technology arrives at $T_d$, the payment efficiency improves for everyone, and it increases in agents’ income. A similar pattern holds when the mobile payment arrives at $T_m$. The intuition why payment efficiency measures (i.e., $x_{T_d}$ and $x_{T_m}$) increase in agents’ income is as follows: It is always feasible for a higher-income agent to mimic a lower-income agent’s adoption behavior. If that turns out to be the optimal decision, the higher-income agent enjoys higher payment efficiency than her lower-income counterpart because the adoption cost (i.e., $k_d$, $k_m$, or $k_m^a$) counts

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20The large-scale introduction of debit cards in the U.S. started in the mid-1980s (see Hayashi, Li, and Wang, 2017), so we set $T_d = T_m - 30$. Note that the simulation results are robust if we use an alternative year for $T_d$ because choosing an earlier (or later) $T_d$ would not change anything except adjusting down (or up) the level of the payment efficiency $x_{T_d}$ given that the card adoption cost $k_d$ counts for a larger (or smaller) share of agents’ income in an earlier (or later) year.
for a smaller share of her income. But if mimicking is not the optimal decision, the higher-income agent must be able to achieve even higher payment efficiency by choosing a payment method different from her lower-income counterpart.

Figure 13 also illustrates how payment efficiency evolves across income levels over time. At time $T_d$, agents either pay or expect to pay in the future the fixed cost $k_d$ to adopt card, and the payment efficiency measure $x_{T_d}$ is a continuous and increasing function of income. Then for any time $t \in (T_d, T_m)$, card users who have paid off $k_d$ in the past no longer count the fixed cost in their payment efficiency measure, so $x_t = 1 - \tau_d$ for them. Meanwhile, cash users who just meet or have not met the card adoption threshold need to pay the fixed cost, so their payment efficiency $x_t$ displays a jump at the card adoption threshold, as illustrated by the green dash-dot curve $\tilde{x}_{T_m}$. For those cash users, their payment efficiency does improve over time due to income growth and thus a declining share of $k_d$ relative to their income. Comparing the two curves $x_{T_m}$ (the red solid one) and $\tilde{x}_{T_m}$ (the green dash-dot one) shows that the introduction of mobile improves payment efficiency for everyone (especially cash users) and makes the jump at the card adoption threshold smaller.21

5.1.2 Aggregate economies

We now take a step further to compare the overall payment efficiency across countries by aggregating over each country’s income distribution. With the exponential income distribution, we can solve explicitly the present-value welfare of aggregate economies, denoted by $W_t(\lambda_t)$, for $t < T_d$ (i.e., cash only), $t = T_d$ (i.e., card becomes available), and $t = T_m$ (i.e., mobile becomes available). Appendix III provides the solution details.

Similar to the discussions above, we define the payment efficiency of an economy, $X_t(\lambda_t)$, as the ratio between the present value of aggregate welfare with and without incurring payment costs at time $t$:

$$X_t(\lambda_t) = \frac{W_t(\lambda_t)}{\frac{\lambda_t}{1 - \beta(1+\gamma)}}. \quad (26)$$

21For cash users, introducing mobile improves their payment efficiency substantially because of the much reduced adoption cost comparing with card (recall that $k_d = 500$ vs. $k_m = 150$). For card users, their payment efficiency only improves slightly somewhere between $1 - \tau_d$ and $1 - \tau_m$ (recall that $\tau_d = 1.4\%$ vs. $\tau_m = 1.395\%$).
Using the parameter values in Table 1, we can now compare payment efficiency across countries under each payment innovation. As before, we assume that the mobile payment technology arrives at $T_m = 2017$, and the card payment arrives at $T_d = T_m - 30$. Figure 14 plots the payment efficiency of each economy for $t < T_d$, $t = T_d$, and $t = T_m$, according to their per capita income level at $T_m$.

![Graph showing payment efficiency by per capita income](image)

**Figure 14. Payment Efficiency by Per Capita Income**

Figure 14 shows that every country has the same payment efficiency when cash is the only payment means (i.e., $X_{t<T_d} = 1 - \tau_h$). Once the card technology arrives, the payment efficiency improves in every country, and the welfare improvement increases in per capita income across countries. Hence, high-income countries gain the most from the card payment adoption. The arrival of mobile payment also benefits every country though disproportionately. As shown in Figure 15, the relative welfare gain $(X_{T_m} - X_{T_d})/X_{T_d}$ peaks for countries with per capita income around $1,600$. Figures 14 and 15 suggest that while the richest countries appear to gain relatively little from their mobile payment adoption, they remain leaders in terms of overall payment efficiency. In contrast, the poorest countries do not gain much from either card or mobile payment innovations, and they lag far behind in overall payment efficiency. Therefore, despite the promise of mobile payments for financial inclusion, its benefits to poorest countries are limited at this stage. In light of this, global financial inclusion may entail further innovations to reduce the payment costs, especially the adoption costs.
5.2 Policy considerations

While our model suggests that the market outcome is socially efficient, the framework that we developed can be extended to discuss policy considerations. For example, we have provided some quantitative analysis in Section 4.2.3 to show that technological progress can be an effective way for advanced economies to restore leading positions in the mobile payment race. To the extent that private firms may not internalize all the social welfare gains in their R&D decisions, government interventions that provide additional R&D incentives could be welfare-improving. Policymakers can also help reduce payment costs with improved regulations.²²

On the other hand, pushing up mobile payment adoption by providing subsidies would cause a welfare loss in our model framework. However, one may argue that such subsidies might be justified, for instance, by some future technological breakthrough based on the mobile payment platform and big data.²³ To facilitate a meaningful cost-and-benefit discussion, our model can be used to estimate the welfare cost of a subsidy policy, and

---

²²For example, the Check 21 Legislation appears to have been instrumental in reducing the costs of checks in the United States (see Humphrey and Hunt, 2013).

²³Another argument for providing adoption subsidies is to encourage early adoption to align the expectations of potential adopters. We will discuss this consideration in Section 6.1, where the model is extended to a two-sided market setting.
we provide a quantitative exercise as follows.

Based on our calibrated model, a country at the U.S. per capita income level in 2017 ($53,356) would on average have a 94.8% card adoption rate and a 19.0% mobile payment adoption rate. Assume that upon the arrival of mobile payment at time $T_m = 2017$, the government offers each mobile payment adopter a subsidy $S$ to reduce the adoption cost, and the subsidy is financed by lump-sum income taxation. Presumably, the subsidy would change the mobile payment adoption thresholds (i.e., $I_m$ and $I^{a}_{m}$) for cash users and card users, but without changing the social costs (i.e., $k_m$ and $k^{a}_{m}$) of adoption. Therefore, we can calculate the present value of social welfare at time $T_m$ under the subsidy by using the new adoption thresholds (cf. Eq. (29) in Appendix III):

$$I_m = \frac{(1 - \beta)(k_m - S)}{(\tau_h - \tau_m)}$$ and $$I^{a}_{m} = \frac{(1 - \beta)(k^{a}_{m} - S)}{(\tau_d - \tau_m)}.$$

Figures 16 and 17 show the effects of such a subsidy. In each figure, we normalize the present value of social welfare under no subsidy to zero. We then plot the change of welfare relative to the no-subsidy benchmark at different subsidy levels, ranging from $0$ to $150$ per adopter. Recall that in our calibration, it costs $100$ for a card user to adopt the card-complementing mobile payment technology, and it costs $150$ for a cash user to adopt the card-substituting one.
Figure 16 reports the overall effects. As the amount of subsidy per adopter rises, mobile payment adoption increases, but welfare falls at an increasing rate. However, the welfare loss slows down and turns almost flat when the subsidy reaches $98 per adopter. Eventually, as the subsidy increases to $150 per adopter, the mobile payment adoption rate reaches 100%, and the welfare loss maximizes at $88.17 per capita. The reason that the maximal welfare loss per capita is smaller than the subsidy per adopter is that a part of the tax used to finance the subsidy is offset by the increased transaction efficiency from using mobile payments.

![Figure 16: Overall Effects of Mobile Payment Subsidy](image)

Figure 17 decomposes the overall subsidy effects between card users and cash users. It becomes clear that most of the subsidy effects come from the card users. In this economy, right before time $T_m$, 94.8% of agents are card users and 5.2% are cash users. Without any subsidy, the mobile payment adoption rate at time $T_m$ would be 19.0%, among which 15.3% are card users and 3.6% are cash users. Should the subsidy per adopter increase and reach $98 per adopter, all the 94.8% card users would have adopted mobile payments, which would lead to a welfare drop of $87.32 per capita. In the meantime, another 4.6% of adopters would come from cash users, resulting in a welfare loss of $0.36 per capita. If the subsidy goes above $98, no further changes would occur from card users, but mobile payment adoption and welfare loss would continue to rise from cash users though the
magnitude would be small. Eventually, when the subsidy reaches $150 per adopter, all the 5.2% cash users would adopt mobile payment, leading to a welfare loss of $0.85 per capita.

The above exercise is based on the assumption that both mobile payment options, the card-complementing one and the card-substituting one, are offered in the country. In an alternative scenario where only the card-complementing option is available, we may just need to exclude the small fraction of the cash-mobile switchers from the calculation. At the end, the quantitative findings, because they are mainly driven by card-mobile switchers, are very similar. In either case, the welfare loss quantified in our analysis provides a benchmark that one may use to compare with mobile payments’ potential future benefits outside our model.

6 Further discussions

While our model fits well the average cross-country pattern of mobile payment adoption, it does not cover all the factors affecting payment adoption decisions. In this section, we extend our model and provide some further discussions.

6.1 Two-sided market considerations

It is well known in the literature that the payment market is two-sided. A payment technology needs to be adopted by both buyers and sellers for being widely used in the economy. Our model so far has been explicit about consumers’ (buyers’) side of the market but not much about the merchants’ (sellers’) side. We now extend our model to a two-sided market setting and explore policy implications.

As before, consider that each consumer receives an income $I_t$ at time $t$, and $I_t$ follows an exponential distribution across the population of consumers. The income is used to purchase a numeraire good for consumption each period. The numeraire good is produced at a unit cost and distributed through competitive merchants. Conducting a transaction between a merchant and a consumer requires using a payment technology $i \in \{h \text{ (cash)}, d \text{ (card)}, m \text{ (mobile)}\}$, for which the merchant (seller) and the consumer (buyer) each incurs a variable cost $\tau_{s,i}$ and $\tau_{b,i}$ per dollar of transactions, respectively. Merchants are each
at a sufficiently large size, so the fixed cost for a merchant to adopt card or mobile payment technology is negligible on a per customer or per transaction basis. Assume merchants can price discriminate based on payment method, for example, by specializing in accepting a particular payment form or charging customers different prices based on payment instruments. Therefore, a competitive merchant accepting payment technology \( i \) would set price \( p_i \) for selling the numeraire good to break even:

\[
p_i = \frac{1}{1 - \tau_{s,i}};
\]

and a consumer using payment technology \( i \) at time \( t \) would purchase and consume the quantity \( q_{i,t} \) of the good:

\[
q_{i,t} = \frac{I_t(1 - \tau_{b,i})}{p_i} = I_t(1 - \tau_{b,i})(1 - \tau_{s,i}).
\]

Assume that consumers need to pay \( k_d \) and \( k_m \) as the one-time fixed costs associated with adopting card and mobile payment technology, respectively. It is straightforward to see the new model setting is equivalent to our original model by changing notations: For each payment technology \( i \in \{h, d, m\} \), we simply need to redefine the variable cost \( \tau_i \) such that

\[
(1 - \tau_i) = (1 - \tau_{b,i})(1 - \tau_{s,i}) \implies \tau_i = \tau_{b,i} + \tau_{s,i} - \tau_{b,i}\tau_{s,i}.
\]

As before, to capture the technology progress between cash, card, and mobile, we assume \( \tau_h > \tau_d > \tau_m \) and \( k_d > k_m \).

Extending our model interpretation to the two-sided market setting brings additional insights. For one thing, the discussion makes it clear that one should take into account payment costs of both merchants and consumers in the analysis. That is the reason why we choose to calibrate our model using measures of social costs of payment means.

Moreover, given that the payment market outcome depends on two sides’ decisions, multiple equilibria can arise. The market outcome we discussed previously remains a valid equilibrium, but it is no longer the unique one. For example, there could exist another equilibrium where no merchant or consumer adopts a new payment technology because they each expect no adoption from the other side. This so-called “chicken-and-egg” dy-
namic often arises in network industries or for technologies featuring strong adoption complementarity, and coordination becomes an important issue (see e.g., Buera et al., 2021). In terms of mobile payments, we observe in the data that some countries have an adoption rate far below their peers with similar per capita income levels, which might result from certain coordination failures among relevant parties. In those cases, appropriate policy interventions, such as coordinating standard setting or providing incentives for early adoption, may help align market expectations and enhance welfare.

The discussion above suggests that our model can apply to a two-sided market setting under the assumption of competitive merchants and price discrimination based on payment method. In the cases where merchants have market power or do not price discriminate based on payment method, things become more complicated (e.g., see Li et al., 2020 for a related analysis), and our model may serve as a simplified first-order approximation. We leave a full-blown two-sided market analysis for future research.

6.2 Kenya, China, and the U.S.

Kenya and China currently are front-runners in mobile payment adoption. Figure 18 suggests that their extraordinary performance may have idiosyncratic components beyond the theory that we offer to explain the average cross-country pattern.

![Figure 18. Model Fit: Kenya, China and the U.S.](image)

For example, Aker, Prina and Welch (2020) show that mobile money has failed to take off in Niger because of a chicken-and-egg problem: Agents need to be widespread for the service to be useful, but putting agents everywhere isn’t viable until the service is widespread.
Note that in our model calibration, we assume that all the countries in the sample share the same set of parameter values, which provides useful model discipline. However, this assumption is not intended to fit outlier cases, and our model provides some clues on how things would differ when relaxing the assumption. According to our model (cf. Eq. (19)), mobile payment adoption would be higher if mobile payment technology is more efficient (i.e., a lower $\tau_m$) or less costly (i.e., a lower $k_m$), or the card technology is less efficient (i.e., a higher $\tau_d$) or more costly (i.e., a higher $k_d$). These factors could be relevant for the Kenya and China discussions. In both countries, it is well known that the banking sectors have been quite inefficient, which suggests a higher $k_d$ or $\tau_d$. In contrast, the mobile payment service providers in each country, Safaricom and Vodafone in Kenya as well as Alibaba and Tencent in China, are very innovative and successful players, which may suggest a lower $k_m$ or $\tau_m$.

Some factors outside our model may also play important roles. For example, our benchmark model does not consider the variation of market structure and government intervention across countries, which may also have driven some of the adoption pattern. Also, our model focuses on the payment aspect of the mobile payment technology, while in reality the new technology may serve multiple functions. For example, Jack and Suri (2014) highlight the role of M-PESA in urban-rural remittances in Kenya, which provides an important risk-sharing function. In China, the two giant tech firms, Tencent and Alibaba, have developed their mobile payment services, WeChat Pay and Alipay, strategically to extend their business models, for instance, to cross-sell consumer and business loan services based on payments data (Hau et al., 2019). It would be very valuable for future research to explore these additional factors.

In comparison, the United States has been lagging in mobile payment adoption. Its performance, however, is in line with the cross-country average pattern explained by our theory. Therefore, our model provides a useful framework for policy discussions in the U.S. context. Our analysis shows that countries like the United States, the previous card

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25 Recent studies suggest that the unique urban-rural remittance pattern in Kenya may help explain its exceptionally wide adoption of M-PESA. Therefore, Kenya’s success in adopting mobile payment should be regarded as an outlier rather than normative (see Piper, Kelsey (September 11, 2020). What Kenya can teach its neighbors — and the US — about improving the lives of the “unbanked.” Vox). This is consistent with our model’s prediction, which underestimates the mobile payment adoption rate of Kenya but fits well the adoption rates of Kenya’s neighboring countries.
payment leaders, naturally tend to fall behind in the mobile payment race. Falling behind can be an optimal choice for such countries because the incremental improvement introduced by the current mobile payment technology does not provide a sufficient incentive for them to switch. In this context, subsidizing mobile payment adoption could cause welfare losses. Instead, policymakers may consider promoting mobile payments in more productive ways, for example, by encouraging greater mobile payment technology progress or reducing market frictions of coordination.

7 Conclusion

This paper provides a quantitative theoretical framework to explain the adoption of card and mobile payments within and across countries. With a novel dataset, we find that the adoption rate of mobile payment has a non-monotonic relationship with per capita income. This is in contrast with the card payment, for which the adoption increases monotonically in per capita income across countries. Also, countries favor different mobile payment solutions: advanced economies favor those complementary to the existing card payments, while developing countries favor those substituting cards.

Our theory provides a consistent explanation for these patterns. In our model, three payment technologies, cash, card, and mobile, arrive sequentially. Newer payment technologies lower the variable costs of conducting payments, but they require a fixed cost to adopt. As a result, rich countries enjoy advantages in adopting card payments for replacing cash early on, but this success later hinders their adoption of the mobile payment innovation. Also, the fixed-cost considerations make it more attractive for card-intensive countries to adopt mobile payment methods complementary to cards, while cash-intensive countries favor card-substituting mobile solutions.

Our model calibration matches cross-country adoption patterns of card and mobile payments well. Based on the quantitative model, we find that lagging behind in mobile payment adoption does not necessarily mean that advanced economies fall behind in overall payment efficiency. Moreover, slower adoption can be an optimal choice given that

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26 As a theoretical benchmark, our model assumes that payment services are provided by competitive firms, while in reality some payment service providers may have market power that distorts payment pricing and adoption. In the latter case, certain government interventions might be warranted.
the incremental benefit of switching from card to the current mobile payment technology is not large enough. Down the road, greater technological advances in mobile payments are needed for advanced economies to regain leading positions in the payment race, and governments may play positive roles in facilitating technological progress and market coordination.

While our paper focuses on payment services, the mobile payment innovation may have impact beyond payments. For example, it may help extend financial services to the unbanked population and reduce poverty. Meanwhile, the rise of nonbank payment service providers, particularly telecom companies and fintech firms, may pose new challenges to financial stability and regulations. Those would be interesting topics for future research. On the other hand, leapfrogging is a relevant issue for the adoption of other major innovations. For example, mobile phones have enabled developing countries to skip the old fixed-line technology and move straight to the mobile technology, and solar energy technologies may allow developing countries to skip an energy infrastructure based on fossil fuels but jump directly into the Solar Age. Our analysis derives conditions for leapfrogging to occur in a payment context, which might help shed light on the broad issue on rank-preserving versus leapfrogging in adopting new technologies.
References


Appendix

I. Data sources.

The mobile payment data introduced in Section 2.2 are drawn from two sources. First, the data on the adoption rate for card-substituting mobile payment services in 2017 are based on the Global Financial Inclusion (Global Findex) Database of the World Bank, which surveyed 76 countries with a visible presence of Mobile Money payment services. The Global Findex database was launched in 2011 and has been published every three years since then. The 2017 version of the database is based on nationally representative surveys of more than 150,000 adults (age 15 and above) in 144 economies. Among the 144 economies, 76 economies (where the GSMA MMU database indicates that mobile money accounts were available at the time the survey was carried out) were surveyed for mobile money adoption: “To identify people with a mobile money account, the 2017 Global Findex survey asked respondents about their use of specific services available in their economy — such as M-PESA, MTN Mobile Money, Airtel Money, or Orange Money — and included in the GSM Association’s Mobile Money for the Unbanked (GSMA MMU) database. The definition of a mobile money account is limited to services that can be used without an account at a financial institution.”

Second, the data on the adoption rate for card-complementing mobile payments around 2017 were gathered from eMarketer’s public website. eMarketer is a market research company headquartered in New York City. Its report on “Proximity Mobile Payment Users Worldwide, 2019” estimates adult mobile proximity payment users (age 14+) in 23 countries where mobile proximity payments had a visible presence. According to the European Payments Council, “mobile proximity payments are mobile payments in which the payer and the payee are in the same location and where the communication between their devices takes place through a proximity technology (such as Near Field Communication (NFC), Quick Response (QR) codes, Bluetooth technology, etc.).” To be more specific, the adoption rate of mobile proximity payments in the eMarketer data is the adoption rate among mobile phone users, so we multiply that by the mobile phone ownership rate of each country (obtained from GSMA) to obtain the mobile proximity
payment adoption rate in the population. As a sanity check, our estimate of the mobile payment adoption rate in the eMarketer data is 24.6% for the United States, comparable to the mobile payment adoption rate of 28.7% estimated from the U.S. Survey of Consumer Payment Choice conducted by the Federal Reserve in 2017.

II. Regression results.

This appendix section provides the regression results related to Figures 4 and 5. Table A1 reports the OLS results for estimating the card and mobile payment adoption. Across the 94 countries in the sample, the regression (1) shows that the card adoption rate in 2017 is significantly and positively related to per capita GDP in 2017. In contrast, the regression (2) shows that the mobile payment adoption bears no significant relationship with per capita GDP for the same sample. In fact, the adjusted $R^2$ shows a negative value, which implies that we would have had a better fit if we simply had run a regression with only a constant. However, a pattern starts to emerge once we remove the countries that have very low adoption rates of mobile payments (i.e., adoption rate < 10%) and group the remaining ones by income. The regression (3) shows that mobile payment adoption increases in per capita GDP for low-income countries (i.e., per capita GDP < $2,500) and high-income countries (i.e., per capita GDP > $30,000), but decreases in per capita GDP for middle-income countries (i.e., $2,500 \leq \text{per capita GDP} \leq $30,000).

Specifically, the coefficient estimate of $\ln(\text{GDP per capita})$ for the low-income countries is 0.113 and statistically significant. This suggests that doubling per capita GDP would increase mobile payment adoption by 11.3% for the low-income countries. The coefficient estimate of $\ln(\text{GDP per capita}) \times 1\{\text{High Income}\}$ is small and not statistically significant, suggesting that the marginal effect of per capita GDP on mobile payment adoption in high-income countries is not different from that in low-income countries. On the other hand, we estimate the coefficient of $\ln(\text{GDP per capita}) \times 1\{\text{Middle Income}\}$ to be -0.163 and statistically significant. This implies that the marginal effect of per capita GDP on mobile payment adoption in middle-income countries is significantly lower than that in low-income (and high-income) countries. The coefficient difference, (0.113-0.163), suggests that doubling per capita GDP is associated with a 5% reduction in mobile payment adoption rate among middle-income countries.
Table A1. Cross-Country Payment Adoption: OLS Regressions

<table>
<thead>
<tr>
<th></th>
<th>Card</th>
<th>Mobile</th>
<th>Mobile</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(1)</td>
<td>(2)</td>
<td>(3)</td>
</tr>
<tr>
<td>ln(GDP per capita)</td>
<td>0.186***</td>
<td>0.001</td>
<td>0.113**</td>
</tr>
<tr>
<td></td>
<td>(0.009)</td>
<td>(0.010)</td>
<td>(0.053)</td>
</tr>
<tr>
<td>ln(GDP per capita) ×1{Middle Income}</td>
<td>-0.163*</td>
<td></td>
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<tr>
<td></td>
<td>(0.084)</td>
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<td></td>
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<td>ln(GDP per capita) ×1{High Income}</td>
<td>-0.007</td>
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<td></td>
</tr>
<tr>
<td></td>
<td>(0.133)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1{Middle Income}</td>
<td>1.197*</td>
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<td></td>
</tr>
<tr>
<td></td>
<td>(0.692)</td>
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<tr>
<td>1{High Income}</td>
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<td></td>
</tr>
<tr>
<td></td>
<td>(1.365)</td>
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<td></td>
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<tr>
<td>Constant</td>
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<td>0.163*</td>
<td>-0.497</td>
</tr>
<tr>
<td></td>
<td>(0.079)</td>
<td>(0.083)</td>
<td>(0.362)</td>
</tr>
<tr>
<td>Observations</td>
<td>94</td>
<td>94</td>
<td>59</td>
</tr>
<tr>
<td>Adjusted $R^2$</td>
<td>0.81</td>
<td>-0.01</td>
<td>0.07</td>
</tr>
</tbody>
</table>

The results in Table A1 are based on the Ordinary Least Squares (OLS) models. The dependent variable is the debit card adoption rate of 2017 in regression (1) or the mobile payment adoption rate around 2017 in regressions (2) and (3). The independent variables include the GDP per capita of 2017 and a constant in regressions (1) and (2), plus two dummy variables (i.e., Middle Income and High Income) and their interaction terms with the GDP per capita in regression (3). Standard errors are reported in the parentheses. *** Significance at 1% level, ** at 5% level, and * at 10% level.

For robustness checks, we re-run the regressions using the Fractional Logit (FL) model to address the fractional nature of the dependent variable, which is bounded by 0 and 1. The estimated marginal effects, shown in Table A2, are very similar to the OLS results in Table A1.

We also re-run the regressions using the Two-Stage Least Squares (2SLS) model to address a potential endogeneity concern that the adoption of a payment innovation may have reverse impact on contemporaneous per capita GDP. To purify the potential reverse impact, we bring in per capita GDP in 2004 (which is more than a decade ago and well before the mobile payment was introduced) as an instrument for per capita GDP in 2017, and the first-stage results are highly significant. The second-stage results, shown in Table A3, are consistent with the OLS findings that card adoption has a positive relationship with per capita income, while mobile payment adoption has a non-monotonic relationship.
Table A2. Cross-Country Payment Adoption: FL Regressions

<table>
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<th>Card</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>(1)</td>
<td>(2)</td>
<td>(3)</td>
</tr>
<tr>
<td>ln(GDP per capita)</td>
<td>0.229***</td>
<td>0.001</td>
<td>0.106***</td>
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<tr>
<td></td>
<td>(0.012)</td>
<td>(0.008)</td>
<td>(0.039)</td>
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<tr>
<td>ln(GDP per capita) × 1{Middle Income}</td>
<td>-0.155**</td>
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</tr>
<tr>
<td></td>
<td></td>
<td>(0.070)</td>
<td></td>
</tr>
<tr>
<td>ln(GDP per capita) × 1{High Income}</td>
<td>0.014</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.061)</td>
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</tr>
<tr>
<td>1{Middle Income}</td>
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<td>1.149*</td>
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<td>1{High Income}</td>
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<td>94</td>
<td>59</td>
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</tbody>
</table>

Regressions in Table A2 are based on the Fractional Logit (FL) models. The dependent and independent variables in the regressions are the same as in Table A1. The coefficient estimates are expressed in terms of marginal effects evaluated at the means of the independent variables. Standard errors are reported in the parentheses. *** Significance at 1% level, ** at 5% level, and * at 10% level.

Table A3. Cross-Country Payment Adoption: 2SLS Regressions
(Second-Stage Results)

<table>
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<tbody>
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<td>(3)</td>
</tr>
<tr>
<td>ln(GDP per capita)</td>
<td>0.186***</td>
<td>0.002</td>
<td>0.100*</td>
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<td>(0.009)</td>
<td>(0.010)</td>
<td>(0.055)</td>
</tr>
<tr>
<td>ln(GDP per capita) × 1{Middle Income}</td>
<td>-0.203**</td>
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<td></td>
<td></td>
<td>(0.087)</td>
<td></td>
</tr>
<tr>
<td>ln(GDP per capita) × 1{High Income}</td>
<td>0.039</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.144)</td>
<td></td>
</tr>
<tr>
<td>1{Middle Income}</td>
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<td></td>
<td>1.592**</td>
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<td></td>
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<td>1{High Income}</td>
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<td>-0.891</td>
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<td>Constant</td>
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<tr>
<td>Observations</td>
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<td>94</td>
<td>59</td>
</tr>
</tbody>
</table>

Regressions in this table are based on the Two-Stage Least Squares (2SLS) models. The dependent and independent variables in the regressions are the same as in Table A1 except that the independent variable ln(GDP per capita 2017) is instrumented by its value of 2004. Standard errors are reported in the parentheses. *** Significance at 1% level, ** at 5% level, and * at 10% level.
III. Present-value welfare of aggregate economies.

This appendix section calculates the present-value welfare of aggregate economies.

Recall that $\bar{V}_h(I)$ is the value function of an agent $I$ who would permanently use the cash technology, given by Eq. (20). Accordingly, the present-value welfare of a pure cash economy, $W_{h,t}$, at any time $t$ is

$$W_{h,t} = \int_0^\infty \bar{V}_h(I) dG_t(I) = \frac{(1 - \tau_h) \lambda_t}{1 - \beta(1 + g)}.$$  \hspace{1cm} (27)

Thus, the present-value welfare of an economy, denoted by $W_t$, equals $W_{h,t}$ for any $t < T_d$.

Recall that $\bar{V}_d(I)$ is the value function of an agent $I$ who would permanently use the card technology, given by Eq. (21). Accordingly, the present-value welfare of the economy, $W_{T_d}$, at time $T_d$ when card technology arrives is

$$W_{T_d} = W_{h,T_d} + \int_{I_d}^\infty (\bar{V}_d(I) - k_d - \bar{V}_h(I)) dG_{T_d}(I) \hspace{1cm} (28)$$

$$+ \sum_{s=1}^\infty \int_{\frac{I_d}{(1+g)^s}}^{I_d} \beta^s (\bar{V}_d(I(1+g)^s) - k_d - \bar{V}_h(I(1+g)^s)) dG_{T_d}(I),$$

where $I_d = \frac{(1-\beta)k_d}{(\tau_h-\tau_d)}$ is given by Eq. (5). Note that the first term of the right-hand side of Eq. (28) is the present value of welfare for all the agents if they continue using cash forever. The second term is the additional welfare gains for card adopters at time $T_d$, and the last term is the additional welfare gains for future card adopters.

Given the exponential distribution $G_{T_d}(I) = 1 - \exp(-I/\lambda_{T_d})$, Eq. (28) yields that

$$W_{T_d} = \frac{(1 - \tau_h) \lambda_{T_d}}{1 - \beta(1 + g)} + \frac{(\tau_h - \tau_d)}{1 - \beta(1 + g)} \int_{I_d}^\infty IdG_{T_d}(I) - k_d \int_{I_d}^\infty dG_{T_d}(I)$$

$$+ \sum_{s=1}^\infty \beta^s \left( \frac{(\tau_h - \tau_d)(1+g)^s}{1 - \beta(1 + g)} \int_{\frac{I_d}{(1+g)^s}}^{I_d} IdG_{T_d}(I) - k_d \sum_{s=1}^\infty \beta^s \int_{\frac{I_d}{(1+g)^s}}^{I_d} dG_{T_d}(I) \right)$$

$$= \frac{(1 - \tau_h) \lambda_{T_d}}{1 - \beta(1 + g)} + \frac{(\tau_h - \tau_d)}{1 - \beta(1 + g)} \exp\left(-\frac{I_d}{\lambda_{T_d}}\right)(\lambda_{T_d} + I_d) - k_d \exp\left(-\frac{I_d}{\lambda_{T_d}}\right)$$

$$+ \sum_{s=1}^\infty \beta^s \left( \frac{(\tau_h - \tau_d)(1+g)^s}{1 - \beta(1 + g)} \left( \exp\left(-\frac{I_d}{(1+g)^s\lambda_{T_d}}\right)(\lambda_{T_d} + \frac{I_d}{(1+g)^s}) - \exp\left(-\frac{I_d}{(1+g)^{s-1}\lambda_{T_d}}\right)\lambda_{T_d} + \frac{I_d}{(1+g)^{s-1}} \right) \right)$$

$$- \sum_{s=1}^\infty \beta^s \left( \frac{I_d}{(1 + g)^s\lambda_{T_d}} - \frac{I_d}{(1 + g)^{s-1}\lambda_{T_d}} \right) k_d.$$
Recall that $\tilde{V}_m(I)$ is the value function of an agent $I$ who would permanently use the mobile payment technology, given by Eq. (23). We can then derive the present value of welfare for the economy, $W_{T_m}$, at time $T_m$ when mobile technology arrives:

$$W_{T_m} = \int_0^{I_d(1+g)} \tilde{V}_h(I)dG_{T_m}(I) + \int_{I_m}^{I_d(1+g)} (\tilde{V}_m(I) - k_m - \tilde{V}_h(I)) dG_{T_m}(I) + \int_{I_d(1+g)}^{\infty} \tilde{V}_d(I)dG_{T_m}(I) + \int_{\max(I_{m'}, I_d(1+g))}^{\infty} (\tilde{V}_m(I) - k_m - \tilde{V}_d(I)) dG_{T_m}(I)$$

where $I_m = \frac{(1-\beta)k_m}{(\tau_h - \tau_m)}$ is given by Eq. (10), and $I_{m'}^a = \frac{(1-\beta)k_m^a}{(\tau_d - \tau_m)}$ is given by Eq. (17). Note that the first term of the right-hand side of Eq. (29) is the present-value welfare for all the cash users at $T_m - 1$ if they continue using cash at time $T_m$ and forever. The second term is the additional welfare gains of cash-mobile switchers at time $T_m$, and the third term is the additional welfare gains for future cash-mobile switchers. The fourth term is the present-value welfare for all the card adopters at $T_m - 1$ if they continue using card at time $T_m$ and forever. The fifth term is the additional welfare gains of card-mobile switchers at time $T_m$, and the last term is the additional welfare gains for future card-mobile switchers.

Denote that $\phi$ satisfies $\frac{I_{m'}^a}{(1+g)^{\phi+1}} > I_d(1+g)$ and $\frac{I_{m'}^a}{(1+g)^{\phi+1}} \leq I_d(1+g)$. Eq. (29) implies

$$W_{T_m} = \frac{(1-\tau_h)}{1-\beta(1+g)} \int_0^{I_d(1+g)} I_dG_{T_m}(I) + \frac{(\tau_h - \tau_m)}{1-\beta(1+g)} \int_{I_m}^{I_d(1+g)} I_dG_{T_m}(I) - k_m \int_{I_m}^{I_d(1+g)} dG_{T_m}(I)$$

$$+ \sum_{s=1}^{\infty} \beta^s \frac{(\tau_h - \tau_m)(1+g)^s}{1-\beta(1+g)} \int_{I_d(1+g)}^{I_{m'}^a \cdot I_d(1+g)} I_dG_{T_m}(I) - k_m \sum_{s=1}^{\infty} \beta^s \int_{I_d(1+g)}^{I_{m'}^a \cdot I_d(1+g)} dG_{T_m}(I)$$

$$+ \frac{(1-\tau_d)}{1-\beta(1+g)} \int_{I_d(1+g)}^{\infty} I_dG_{T_m}(I) + \frac{(\tau_d - \tau_m)}{1-\beta(1+g)} \int_{I_{m'}^a \cdot I_d(1+g)}^{\infty} I_dG_{T_m}(I) - k_m \int_{I_{m'}^a \cdot I_d(1+g)}^{\infty} dG_{T_m}(I)$$

$$+ \sum_{s=1}^{\phi} \beta^s \frac{(\tau_d - \tau_m)(1+g)^s}{1-\beta(1+g)} \int_{I_{m'}^a \cdot I_d(1+g)}^{I_{m'}^a \cdot I_d(1+g)} I_dG_{T_m}(I) - k_m \sum_{s=1}^{\phi} \beta^s \int_{I_{m'}^a \cdot I_d(1+g)}^{I_{m'}^a \cdot I_d(1+g)} dG_{T_m}(I)$$

$$+ \beta^{\phi+1} \frac{(\tau_d - \tau_m)(1+g)^{\phi+1}}{1-\beta(1+g)} \int_{I_d(1+g)}^{I_{m'}^a \cdot I_d(1+g)} I_dG_{T_m}(I) - k_m \beta^{\phi+1} \int_{I_d(1+g)}^{I_{m'}^a \cdot I_d(1+g)} dG_{T_m}(I).$$
\[ W_{T_m} = \frac{(1 - \tau_h)}{1 - \beta(1 + g)} \left( \lambda_{T_m} - \exp\left(-\frac{I_d(1 + g)}{\lambda_{T_m}}\right)(\lambda_{T_m} + I_d(1 + g)) \right) \\
+ \frac{(\tau_h - \tau_m)}{1 - \beta(1 + g)} \left( \exp\left(-\frac{I_m}{\lambda_{T_m}}\right)(\lambda_{T_m} + I_m) - \exp\left(-\frac{I_d(1 + g)}{\lambda_{T_m}}\right)(\lambda_{T_m} + I_d(1 + g)) \right) \\
- k_m \left( \exp\left(-\frac{I_m}{\lambda_{T_m}}\right) - \exp\left(-\frac{I_d(1 + g)}{\lambda_{T_m}}\right) \right) \\
+ \sum_{s=1}^{\infty} \beta^s \left( \frac{(\tau_h - \tau_m)(1 + g)^s}{1 - \beta(1 + g)} \right) \left( \exp\left(-\frac{I_m}{(1 + g)^s\lambda_{T_m}}\right)(\lambda_{T_m} + I_m) - \exp\left(-\frac{I_d(1 + g)}{(1 + g)^s\lambda_{T_m}}\right)(\lambda_{T_m} + I_d(1 + g)) \right) \\
- k_m \sum_{s=1}^{\infty} \beta^s \left( \frac{I_m}{(1 + g)^s\lambda_{T_m}} \right) - \exp\left(-\frac{I_d}{(1 + g)^s\lambda_{T_m}}\right)(\lambda_{T_m} + I_d(1 + g)) \\
+ \frac{(1 - \tau_d)}{1 - \beta(1 + g)} \exp\left(-\frac{I_d(1 + g)}{\lambda_{T_m}}\right)(\lambda_{T_m} + I_d(1 + g)) \\
+ \frac{(\tau_d - \tau_m)}{1 - \beta(1 + g)} \exp\left(-\frac{I_m'}{\lambda_{T_m}}\right)(\lambda_{T_m} + I_m') - k_m \exp\left(-\frac{I_m'}{\lambda_{T_m}}\right) \\
+ \sum_{s=1}^{\phi} \beta^s \frac{(\tau_d - \tau_m)(1 + g)^s}{1 - \beta(1 + g)} \left( \exp\left(-\frac{I_m'}{(1 + g)^s\lambda_{T_m}}\right)(\lambda_{T_m} + I_m') - \exp\left(-\frac{I_m'}{(1 + g)^s\lambda_{T_m}}\right)(\lambda_{T_m} + I_m') \right) \\
- k_m \sum_{s=1}^{\phi} \beta^s \left( \frac{I_m'}{(1 + g)^s\lambda_{T_m}} \right) - \exp\left(-\frac{I_m'}{(1 + g)^s\lambda_{T_m}}\right)(\lambda_{T_m} + I_m') \\
+ \beta^{\phi+1} \frac{(\tau_d - \tau_m)(1 + g)^{\phi+1}}{1 - \beta(1 + g)} \left( \exp\left(-\frac{I_d(1 + g)}{\lambda_{T_m}}\right)(\lambda_{T_m} + I_d(1 + g)) - \exp\left(-\frac{I_m'}{(1 + g)^{\phi+1}\lambda_{T_m}}\right)(\lambda_{T_m} + I_m') \right) \\
- k_m \beta^{\phi+1} \left( \frac{I_d(1 + g)}{\lambda_{T_m}} - \frac{I_m'}{(1 + g)^{\phi+1}\lambda_{T_m}} \right). \]